Chapter 13 Questions to Guide Your Review

- **1.** State the rules for differentiating and integrating vector functions. Give examples.
- **2.** How do you define and calculate the velocity, speed, direction of motion, and acceleration of a body moving along a sufficiently differentiable space curve? Give an example.
- **3.** What is special about the derivatives of vector functions of constant length? Give an example.
- **4.** What are the vector and parametric equations for ideal projectile motion? How do you find a projectile's maximum height, flight time, and range? Give examples.
- **5.** How do you define and calculate the length of a segment of a smooth space curve? Give an example. What mathematical assumptions are involved in the definition?

- **6.** How do you measure distance along a smooth curve in space from a preselected base point? Give an example.
- 7. What is a differentiable curve's unit tangent vector? Give an example.
- **8.** Define curvature, circle of curvature (osculating circle), center of curvature, and radius of curvature for twice-differentiable curves in the plane. Give examples. What curves have zero curvature? Constant curvature?
- **9.** What is a plane curve's principal normal vector? When is it defined? Which way does it point? Give an example.
- **10.** How do you define N and κ for curves in space? How are these quantities related? Give examples.

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- **11.** What is a curve's binormal vector? Give an example. How is this vector related to the curve's torsion? Give an example.
- **12.** What formulas are available for writing a moving body's acceleration as a sum of its tangential and normal components? Give an

example. Why might one want to write the acceleration this way? What if the body moves at a constant speed? At a constant speed around a circle?

13. State Kepler's laws. To what phenomena do they apply?