

## THERMODYNAMIC FUNCTIONS AND RELATIONS

$p$  = pressure       $V$  = volume       $T$  = temperature

$n_i$  = amount of substance  $i$

$x_i = n_i / \sum_j n_j$  = mole fraction of substance  $i$

Energy	$U$
Entropy	$S$
Enthalpy	$H = U + pV$
Helmholtz energy	$A = U - TS$
Gibbs energy	$G = U + pV - TS$
Isobaric heat capacity	$C_p = (\partial H / \partial T)_p$
Isochoric heat capacity	$C_v = (\partial U / \partial T)_v$
Isobaric expansivity	$\alpha = V^{-1}(\partial V / \partial T)_p$
Isothermal compressibility	$\kappa_T = -V^{-1}(\partial V / \partial p)_T$
Isentropic compressibility	$\kappa_S = -V^{-1}(\partial V / \partial p)_S$
	$\kappa_T - \kappa_S = T\alpha^2 V / C_p$
	$C_p - C_v = T\alpha^2 V / \kappa_T$
Gibbs-Helmholtz equation	$H = G - T(\partial G / \partial T)_p$
Maxwell relations	$(\partial S / \partial p)_T = -(\partial V / \partial T)_p$
	$(\partial S / \partial V)_T = -(\partial p / \partial T)_v$
Joule-Thomson expansion	$\mu_{JT} = (\partial T / \partial p)_H = -\{V - T(\partial V / \partial T)_p\} / C_p$
	$\Phi_{JT} = (\partial H / \partial p)_T = V - T(\partial V / \partial T)_p$
Partial molar quantity	$X_i = (\partial X / \partial n_i)_{T,p,n_j \neq i}$
Chemical potential	$\mu_i = (\partial G / \partial n_i)_{T,p,n_j \neq i}$
Perfect gas [symbol <sup>pg</sup> ]	$pV = (\sum_i n_i)RT$
	$\mu_i^{pg} = \mu_i^\theta + RT \ln(x_i p / p^\theta)$
Fugacity	$f_i = (x_i p) \exp\{(\mu_i - \mu_i^{pg}) / RT\}$
Activity coefficient	$\gamma_i = f_i / (x_i f_i^\theta)$
Gibbs-Duhem relation	$0 = SdT - Vdp + \sum_i n_i d\mu_i$

[Superscript  $\theta$  in above equations indicates standard state]

Notation for chemical and physical changes ( $X = H, S, G$ , etc.):

Chemical reaction	$\Delta_r X$
Formation from elements	$\Delta_f X$
Combustion	$\Delta_c X$
Fusion (cry $\rightarrow$ liq)	$\Delta_{fus} X$
Vaporization (liq $\rightarrow$ gas)	$\Delta_{vap} X$
Sublimation (cry $\rightarrow$ gas)	$\Delta_{sub} X$
Phase transition	$\Delta_{trs} X$
Solution	$\Delta_{sol} X$
Mixing	$\Delta_{mix} X$
Dilution	$\Delta_{dil} X$