## SOLUBILITY PRODUCT CONSTANTS

The solubility product constant  $K_{\rm sp}$  is a useful parameter for calculating the aqueous solubility of sparingly soluble compounds under various conditions. It may be determined by direct measurement or calculated from the standard Gibbs energies of formation  $\Delta_{\rm f}G^{\circ}$  of the species involved at their standard states. Thus if  $K_{\rm sp} = [{\rm M}^+]^m$ ,  $[{\rm A}^-]^n$  is the equilibrium constant for the reaction

$$M_{...}A_{..}(s) \rightleftharpoons mM^{+}(aq) + nA^{-}(aq),$$

where  $M_m A_n$  is the slightly soluble substance and  $M^+$  and  $A^-$  are the ions produced in solution by the dissociation of  $M_m A_n$ , then the Gibbs energy change is

$$\Delta G^{\circ} = m \Delta_{r} G^{\circ} (M^{+}, aq) + n \Delta_{r} G^{\circ} (A^{-}, aq) - \Delta_{r} G^{\circ} (M_{u}, A_{u}, s)$$

The solubility product constant is calculated from the equation

$$\ln K_{\rm ep} = -\Delta G^{\circ}/RT$$

The first table below gives selected values of  $K_{\rm sp}$  at 25°C. Many of these have been calculated from standard state thermodynamic data in References 1 and 2; other values are taken from publications of the IUPAC Solubility Data Project (References 3 to 7).

The above formulation is not convenient for treating sulfides because the  $S^{-2}$  ion is usually not present in significant concentrations (see Reference 8). This is due to the hydrolysis reaction

$$S^{-2} + H_2O \rightleftharpoons HS^- + OH^-$$

Compound	Formula	$K_{sp}$
Aluminum phosphate	$AlPO_4$	$9.84 \cdot 10^{-21}$
Barium bromate	Ba(BrO <sub>3</sub> ) <sub>2</sub>	$2.43\cdot10^{-4}$
Barium carbonate	BaCO <sub>3</sub>	$2.58 \cdot 10^{-9}$
Barium chromate	BaCrO <sub>4</sub>	$1.17 \cdot 10^{-10}$
Barium fluoride	BaF <sub>2</sub>	$1.84\cdot10^{-7}$
Barium hydroxide octahydrate	$Ba(OH)_2 \cdot 8H_2O$	$2.55\cdot 10^{-4}$
Barium iodate	Ba(IO <sub>3</sub> ) <sub>2</sub>	$4.01\cdot10^{-9}$
Barium iodate monohydrate	$Ba(IO_3)_2 \cdot H_2O$	$1.67 \cdot 10^{-9}$
Barium molybdate	$BaMoO_4$	$3.54\cdot10^{-8}$
Barium nitrate	$Ba(NO_3)_2$	$4.64\cdot10^{-3}$
Barium selenate	$BaSeO_4$	$3.40\cdot10^{-8}$
Barium sulfate	BaSO <sub>4</sub>	$1.08 \cdot 10^{-10}$
Barium sulfite	BaSO <sub>3</sub>	$5.0\cdot10^{\scriptscriptstyle -10}$
Beryllium hydroxide	Be(OH) <sub>2</sub>	$6.92 \cdot 10^{-22}$
Bismuth arsenate	$BiAsO_4$	$4.43 \cdot 10^{-10}$
Bismuth iodide	$BiI_3$	$7.71 \cdot 10^{-19}$
Cadmium arsenate	$Cd_3(AsO_4)_2$	$2.2\cdot10^{\scriptscriptstyle{-33}}$
Cadmium carbonate	CdCO <sub>3</sub>	$1.0 \cdot 10^{-12}$
Cadmium fluoride	$CdF_2$	$6.44\cdot10^{\scriptscriptstyle -3}$
Cadmium hydroxide	Cd(OH) <sub>2</sub>	$7.2\cdot10^{\scriptscriptstyle -15}$
Cadmium iodate	$Cd(IO_3)_2$	$2.5\cdot10^{-8}$
Cadmium oxalate trihydrate	$CdC_2O_4 \cdot 3H_2O$	$1.42\cdot10^{-8}$
Cadmium phosphate	$Cd_3(PO_4)_2$	$2.53\cdot10^{-33}$
Calcium carbonate (calcite)	CaCO <sub>3</sub>	$3.36 \cdot 10^{-9}$
Calcium fluoride	CaF <sub>2</sub>	$3.45\cdot 10^{-11}$
Calcium hydroxide	Ca(OH) <sub>2</sub>	$5.02\cdot10^{-6}$

which is strongly shifted to the right except in very basic solutions. Furthermore, the equilibrium constant for this reaction, which depends on the second ionization constant of  $H_2S$ , is poorly known. Therefore it is more useful in the case of sulfides to define a different solubility product  $K_{\rm soa}$  based on the reaction

$$M_m S_n(s) + 2H^+ \rightleftharpoons mM^+ + nH_2S$$
 (aq)

Values of  $K_{\rm spa}$ , taken from Reference 8, are given for several sulfides in the auxiliary table following the main table. Additional discussion of sulfide equilibria may be found in References 7 and 9.

## References

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Compound	Formula	$K_{sp}$
Calcium iodate	Ca(IO <sub>3</sub> ) <sub>2</sub>	$6.47 \cdot 10^{-6}$
Calcium iodate hexahydrate	$Ca(IO_3)_2 \cdot 6H_2O$	$7.10\cdot10^{\scriptscriptstyle -7}$
Calcium molybdate	CaMoO <sub>4</sub>	$1.46\cdot10^{-8}$
Calcium oxalate monohydrate	$CaC_2O_4 \cdot H_2O$	$2.32\cdot10^{-9}$
Calcium phosphate	$Ca_3(PO_4)_2$	$2.07 \cdot 10^{-33}$
Calcium sulfate	CaSO <sub>4</sub>	$4.93\cdot10^{\scriptscriptstyle -5}$
Calcium sulfate dihydrate	CaSO <sub>4</sub> · 2H <sub>2</sub> O	$3.14\cdot10^{\scriptscriptstyle -5}$
Calcium sulfite hemihydrate	$CaSO_3 \cdot 0.5H_2O$	$3.1\cdot 10^{-7}$
Cesium perchlorate	CsClO <sub>4</sub>	$3.95\cdot10^{\scriptscriptstyle -3}$
Cesium periodate	CsIO <sub>4</sub>	$5.16\cdot10^{-6}$
Cobalt(II) arsenate	$Co_3(AsO_4)_2$	$6.80 \cdot 10^{-29}$
Cobalt(II) hydroxide (blue)	Co(OH) <sub>2</sub>	$5.92\cdot10^{\scriptscriptstyle -15}$
Cobalt(II) iodate dihydrate	$Co(IO_3)_2 \cdot 2H_2O$	$1.21\cdot10^{\scriptscriptstyle -2}$
Cobalt(II) phosphate	$Co_3(PO_4)_2$	$2.05\cdot10^{\scriptscriptstyle -35}$
Copper(I) bromide	CuBr	$6.27 \cdot 10^{-9}$
Copper(I) chloride	CuCl	$1.72\cdot10^{-7}$
Copper(I) cyanide	CuCN	$3.47 \cdot 10^{-20}$
Copper(I) iodide	CuI	$1.27\cdot 10^{-12}$
Copper(I) thiocyanate	CuSCN	$1.77 \cdot 10^{-13}$
Copper(II) arsenate	$Cu_3(AsO_4)_2$	$7.95\cdot10^{\scriptscriptstyle -36}$
Copper(II) iodate monohydrate	$Cu(IO_3)_2 \cdot H_2O$	$6.94 \cdot 10^{-8}$
Copper(II) oxalate	CuC <sub>2</sub> O <sub>4</sub>	$4.43 \cdot 10^{-10}$
Copper(II) phosphate	$Cu_3(PO_4)_2$	$1.40\cdot10^{\scriptscriptstyle -37}$
Europium(III) hydroxide	Eu(OH) <sub>3</sub>	$9.38\cdot10^{\scriptscriptstyle -27}$
Gallium(III) hydroxide	Ga(OH) <sub>3</sub>	$7.28\cdot10^{\scriptscriptstyle -36}$
Iron(II) carbonate	FeCO <sub>3</sub>	$3.13\cdot 10^{-11}$

Compound	Formula	$K_{sp}$	Compound	Formula	$K_{sp}$
Iron(II) fluoride	FeF,	$2.36 \cdot 10^{-6}$	Radium iodate	Ra(IO <sub>3</sub> ) <sub>2</sub>	1.16 · 10 <sup>-9</sup>
Iron(II) hydroxide	Fe(OH),	$4.87 \cdot 10^{-17}$	Radium sulfate	RaSO <sub>4</sub>	$3.66 \cdot 10^{-11}$
Iron(III) hydroxide	Fe(OH) <sub>3</sub>	$2.79 \cdot 10^{-39}$	Rubidium perchlorate	RbClO <sub>4</sub>	$3.00 \cdot 10^{-3}$
Iron(III) phosphate dihydrate	FePO <sub>4</sub> · 2H <sub>2</sub> O	$9.91 \cdot 10^{-16}$	Scandium fluoride	ScF <sub>3</sub>	$5.81\cdot10^{-24}$
Lanthanum iodate	La(IO <sub>3</sub> ) <sub>3</sub>	$7.50 \cdot 10^{-12}$	Scandium hydroxide	Sc(OH) <sub>3</sub>	$2.22\cdot10^{\scriptscriptstyle -31}$
Lead(II) bromide	PbBr <sub>2</sub>	$6.60 \cdot 10^{-6}$	Silver(I) acetate	AgCH <sub>3</sub> COO	$1.94\cdot10^{\scriptscriptstyle -3}$
Lead(II) carbonate	PbCO <sub>3</sub>	$7.40 \cdot 10^{-14}$	Silver(I) arsenate	$Ag_3AsO_4$	$1.03 \cdot 10^{-22}$
Lead(II) chloride	PbCl <sub>2</sub>	$1.70 \cdot 10^{-5}$	Silver(I) bromate	AgBrO <sub>3</sub>	$5.38\cdot10^{-5}$
Lead(II) fluoride	PbF <sub>2</sub>	$3.3 \cdot 10^{-8}$	Silver(I) bromide	AgBr	$5.35\cdot10^{\scriptscriptstyle -13}$
Lead(II) hydroxide	Pb(OH),	$1.43 \cdot 10^{-20}$	Silver(I) carbonate	Ag <sub>2</sub> CO <sub>3</sub>	$8.46 \cdot 10^{-12}$
Lead(II) iodate	Pb(IO <sub>3</sub> ) <sub>2</sub>	$3.69 \cdot 10^{-13}$	Silver(I) chloride	AgCl	$1.77\cdot 10^{-10}$
Lead(II) iodide	PbI <sub>2</sub>	9.8 · 10-9	Silver(I) chromate	Ag <sub>2</sub> CrO <sub>4</sub>	$1.12 \cdot 10^{-12}$
Lead(II) selenate	PbSeO <sub>4</sub>	$1.37 \cdot 10^{-7}$	Silver(I) cyanide	AgCN	$5.97 \cdot 10^{-17}$
Lead(II) sulfate	PbSO <sub>4</sub>	$2.53 \cdot 10^{-8}$	Silver(I) iodate	AgIO <sub>3</sub>	$3.17\cdot10^{-8}$
Lithium carbonate	Li <sub>2</sub> CO <sub>3</sub>	$8.15 \cdot 10^{-4}$	Silver(I) iodide	AgI	$8.52 \cdot 10^{-17}$
Lithium fluoride	LiF	$1.84\cdot10^{-3}$	Silver(I) oxalate	$Ag_2C_2O_4$	$5.40 \cdot 10^{-12}$
Lithium phosphate	Li <sub>3</sub> PO <sub>4</sub>	$2.37 \cdot 10^{-11}$	Silver(I) phosphate	$Ag_3PO_4$	$8.89 \cdot 10^{-17}$
Magnesium carbonate	MgCO <sub>3</sub>	$6.82 \cdot 10^{-6}$	Silver(I) sulfate	$Ag_2SO_4$	$1.20\cdot10^{\scriptscriptstyle -5}$
Magnesium carbonate	$MgCO_3 \cdot 3H_2O$	$2.38 \cdot 10^{-6}$	Silver(I) sulfite	$Ag_2SO_3$	$1.50 \cdot 10^{-14}$
trihydrate			Silver(I) thiocyanate	AgSCN	$1.03\cdot 10^{-12}$
Magnesium carbonate	$MgCO_3 \cdot 5H_2O$	$3.79 \cdot 10^{-6}$	Strontium arsenate	$Sr_3(AsO_4)_2$	$4.29 \cdot 10^{-19}$
pentahydrate		7.4.5.40.11	Strontium carbonate	SrCO <sub>3</sub>	$5.60 \cdot 10^{-10}$
Magnesium fluoride	MgF <sub>2</sub>	5.16 · 10 <sup>-11</sup>	Strontium fluoride	SrF <sub>2</sub>	$4.33\cdot10^{-9}$
Magnesium hydroxide	Mg(OH) <sub>2</sub>	5.61 · 10 <sup>-12</sup>	Strontium iodate	$Sr(IO_3)_2$	$1.14\cdot10^{-7}$
Magnesium oxalate dihydrate	$MgC_2O_4 \cdot 2H_2O$	4.83 · 10 <sup>-6</sup>	Strontium iodate	$Sr(IO_3)_2 \cdot H_2O$	$3.77\cdot10^{-7}$
Magnesium phosphate	$Mg_3(PO_4)_2$	$1.04 \cdot 10^{-24}$	monohydrate		
Manganese(II) carbonate	MnCO <sub>3</sub>	$2.24 \cdot 10^{-11}$	Strontium iodate hexahydrate	$Sr(IO_3)_2 \cdot 6H_2O$	$4.55 \cdot 10^{-7}$
Manganese(II) iodate	Mn(IO <sub>3</sub> ) <sub>2</sub>	$4.37 \cdot 10^{-7}$	Strontium sulfate	$SrSO_4$	$3.44 \cdot 10^{-7}$
Manganese(II) oxalate dihydrate	$MnC_2O_4 \cdot 2H_2O$	$1.70 \cdot 10^{-7}$	Thallium(I) bromate	TlBrO <sub>3</sub>	$1.10 \cdot 10^{-4}$
Mercury(I) bromide	Hg <sub>2</sub> Br <sub>2</sub>	$6.40 \cdot 10^{-23}$	Thallium(I) bromide	TlBr	$3.71 \cdot 10^{-6}$
Mercury(I) carbonate	Hg <sub>2</sub> CO <sub>3</sub>	$3.6 \cdot 10^{-17}$	Thallium(I) chloride	TlCl	$1.86 \cdot 10^{-4}$
Mercury(I) chloride	Hg <sub>2</sub> Cl <sub>2</sub>	$1.43 \cdot 10^{-18}$	Thallium(I) chromate	Tl <sub>2</sub> CrO <sub>4</sub>	$8.67 \cdot 10^{-13}$
Mercury(I) fluoride	Hg <sub>2</sub> F <sub>2</sub>	$3.10 \cdot 10^{-6}$	Thallium(I) iodate	$TliO_3$	$3.12 \cdot 10^{-6}$
Mercury(I) iodide	Hg <sub>2</sub> I <sub>2</sub>	$5.2 \cdot 10^{-29}$	Thallium(I) iodide	TlI	$5.54\cdot10^{-8}$
Mercury(I) oxalate	$Hg_2C_2O_4$	$1.75 \cdot 10^{-13}$	Thallium(I) thiocyanate	TISCN	$1.57 \cdot 10^{-4}$
Mercury(I) sulfate	Hg <sub>2</sub> SO <sub>4</sub>	$6.5 \cdot 10^{-7}$	Thallium(III) hydroxide	Tl(OH) <sub>3</sub>	$1.68 \cdot 10^{-44}$
Mercury(I) thiocyanate	$Hg_2(SCN)_2$	$3.2 \cdot 10^{-20}$	Tin(II) hydroxide	Sn(OH) <sub>2</sub>	$5.45 \cdot 10^{-27}$
Mercury(II) bromide	HgBr <sub>2</sub>	$6.2 \cdot 10^{-20}$	Yttrium carbonate	$Y_2(CO_3)_3$	$1.03 \cdot 10^{-31}$
Mercury(II) iodide	HgI <sub>2</sub>	$2.9 \cdot 10^{-29}$	Yttrium fluoride	$YF_3$	$8.62 \cdot 10^{-21}$
Neodymium carbonate	$Nd_2(CO_3)_3$	$1.08 \cdot 10^{-33}$	Yttrium hydroxide	Y(OH) <sub>3</sub>	$1.00 \cdot 10^{-22}$
Nickel(II) carbonate	NiCO <sub>3</sub>	$1.42 \cdot 10^{-7}$	Yttrium iodate	$Y(IO_3)_3$	$1.12 \cdot 10^{-10}$
Nickel(II) hydroxide	Ni(OH),	$5.48 \cdot 10^{-16}$	Zinc arsenate	$\operatorname{Zn_3(AsO_4)_2}$	$2.8 \cdot 10^{-28}$
Nickel(II) iodate	Ni(IO <sub>3</sub> ) <sub>2</sub>	$4.71 \cdot 10^{-5}$	Zinc carbonate	ZnCO <sub>3</sub>	$1.46 \cdot 10^{-10}$
Nickel(II) phosphate	$Ni_3(PO_4)_2$	$4.74 \cdot 10^{-32}$	Zinc carbonate monohydrate	$ZnCO_3 \cdot H_2O$	$5.42 \cdot 10^{-11}$
Palladium(II) thiocyanate	$Pd(SCN)_2$	$4.39 \cdot 10^{-23}$	Zinc fluoride	$ZnF_2$	$3.04 \cdot 10^{-2}$
Potassium	K <sub>2</sub> PtCl <sub>6</sub>	$7.48 \cdot 10^{-6}$	Zinc hydroxide	Zn(OH) <sub>2</sub>	$3 \cdot 10^{-17}$
hexachloroplatinate	26		Zinc iodate dihydrate	$Zn(IO_3)_2 \cdot 2H_2O$	$4.1 \cdot 10^{-6}$
Potassium perchlorate	KClO <sub>4</sub>	$1.05 \cdot 10^{-2}$	Zinc oxalate dihydrate	$ZnC_2O_4 \cdot 2H_2O$	$1.38 \cdot 10^{-9}$
Potassium periodate	KIO <sub>4</sub>	$3.71 \cdot 10^{-4}$	Zinc selenide	ZnSe	$3.6 \cdot 10^{-26}$
Praseodymium hydroxide	Pr(OH) <sub>3</sub>	$3.39 \cdot 10^{-24}$	Zinc selenite monohydrate	$ZnSeO_3 \cdot H_2O$	$1.59 \cdot 10^{-7}$
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Sulfides		
Compound	Formula	$K_{_{ m spa}}$
Cadmium sulfide	CdS	$8 \cdot 10^{-7}$
Copper(II) sulfide	CuS	$6\cdot 10^{-16}$
Iron(II) sulfide	FeS	$6\cdot 10^2$
Lead(II) sulfide	PbS	$3\cdot 10^{-7}$
Manganese(II) sulfide (green)	MnS	$3\cdot 10^7$
Mercury(II) sulfide (red)	HgS	$4\cdot 10^{-33}$
Mercury(II) sulfide (black)	HgS	$2\cdot 10^{-32}$
Silver(I) sulfide	$Ag_2S$	$6\cdot 10^{-30}$
Tin(II) sulfide	SnS	$1\cdot 10^{-5}$
Zinc sulfide (sphalerite)	ZnS	$2\cdot 10^{-4}$
Zinc sulfide (wurtzite)	ZnS	$3\cdot 10^{-2}$