

Tutorial on IC Engines for Aircraft

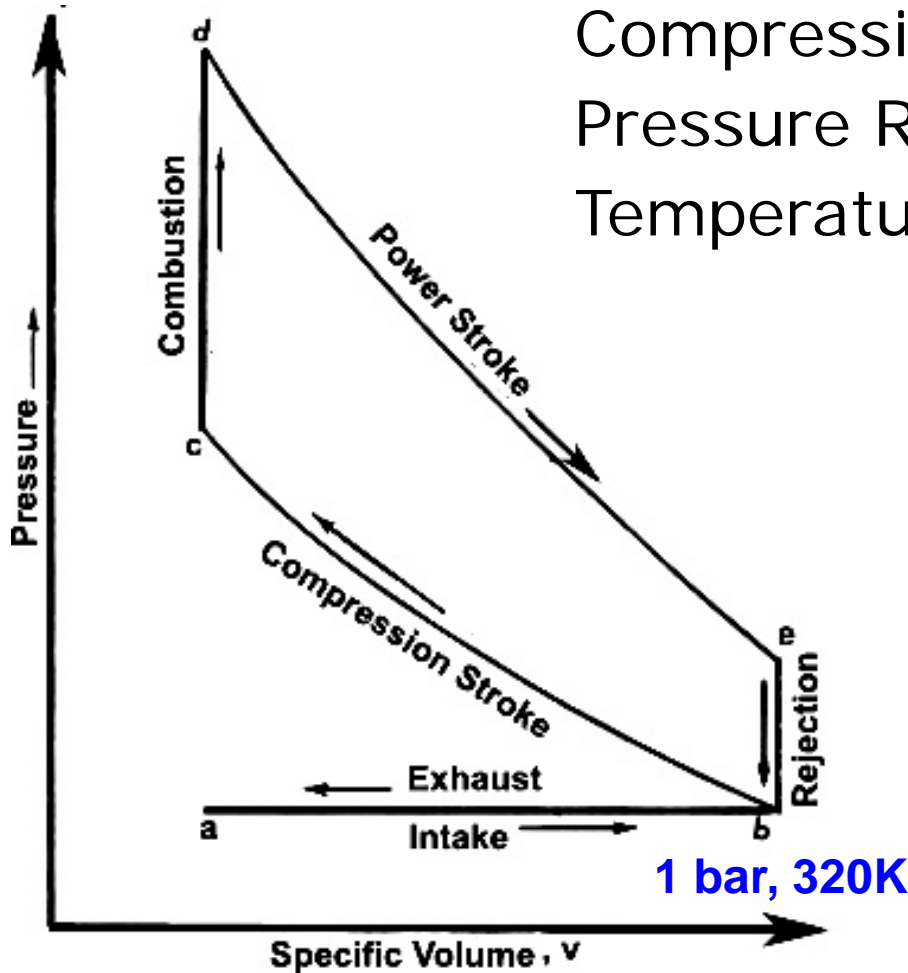
INTRODUCTION TO AEROSPACE PROPULSION

1) For an ideal cycle of a reciprocating IC engine , in which heat is added to the working medium, air, at constant volume, the following working conditions are given : $P_a = 1$ bar, $T_a = 320$ K, Compression ratio = 4.0, gas constant of air, $R = 287$ J/kg.deg; Pressure ratio = 4.0 adiabatic exponent, $k = 1.4$.

For 1 kg of working medium find out :

- a) Amounts of heat added and heat rejected
- b) Thermal efficiency of a Carnot cycle for the given working conditions
- c) Thermal efficiency of the cycle
- d) The Indicated mean effective pressure (**IMEP**)

INTRODUCTION TO AEROSPACE PROPULSION



Compression ratio : $\epsilon = v_b / v_c = 4$
Pressure Ratio : $\pi = p_d / p_c = 4$
Temperature Ratio: $\tau = T_d / T_b = ?$

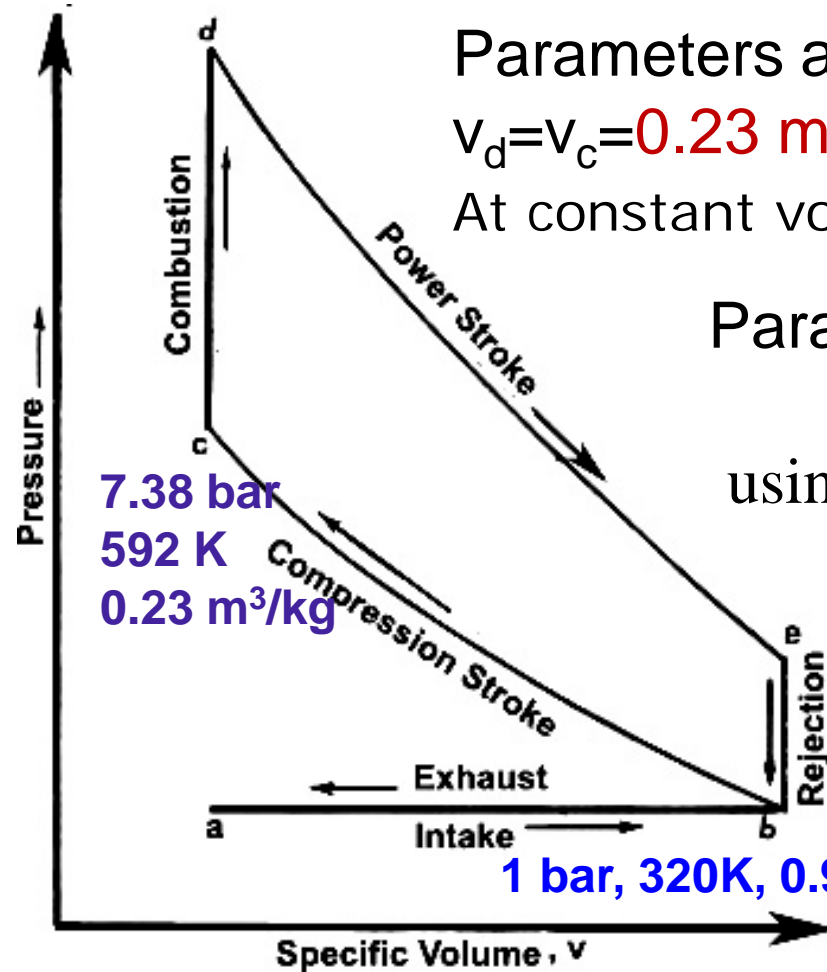
$$v_b = R \cdot T_b / P_b = 287 \times 320 / 10^5 = \mathbf{0.92 \text{ m}^3/\text{kg}}$$

$$v_c = v_b / \epsilon = 0.92 / 4.0 = \mathbf{0.23 \text{ m}^3/\text{kg}}$$

$$p_c = p_b \cdot \epsilon^\kappa = 1 \times 4^{1.4} = \mathbf{7.38 \text{ bar}}$$

$$T_c = p_c \cdot v_c / R = 7.38 \times 10^5 \times 0.23 / 287 = \mathbf{592 \text{ K}}$$

INTRODUCTION TO AEROSPACE PROPULSION



Parameters at point **d** shall be computed from :
 $v_d = v_c = 0.23 \text{ m}^3/\text{kg}$; & $p_d = p_c \times \pi = 7.38 \times 4 = 29.6 \text{ bar}$
 At constant vol., $T_d = T_c \times \pi = 592 \times 4 = 2368 \text{ K}$

Parameters at point **e** may be found :

$$\text{using } \frac{T_e}{T_d} = \left(\frac{v_d}{v_e} \right)^{k-1} = \left(\frac{v_b}{v_c} \right)^{k-1} = \frac{1}{\epsilon^{k-1}}$$

$$T_e = T_d / \epsilon^{k-1} = 2368 / 4^{0.4} = 1340 \text{ K}$$

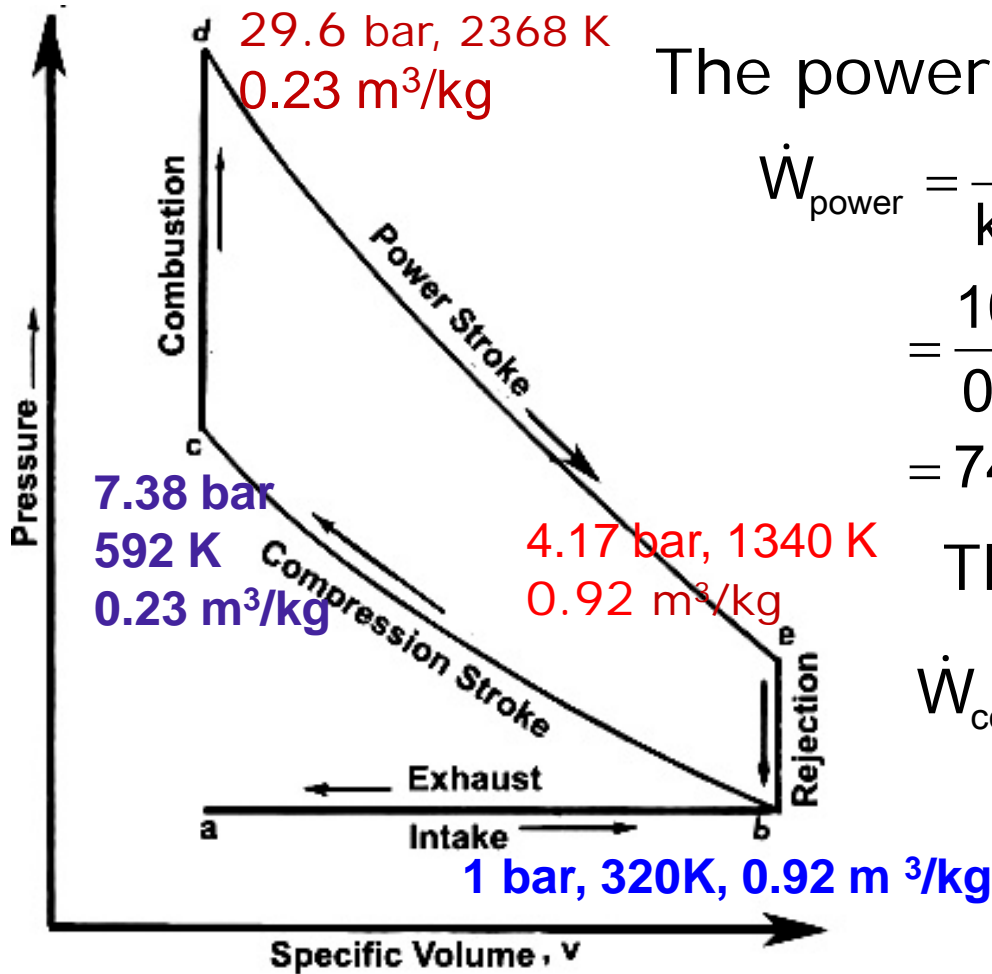
$$v_e = v_b = 0.92 \text{ m}^3/\text{kg}$$

$$P_e = RT_e / v_e$$

$$= 287 \times 1340 / 0.92 \times 10^5$$

$$= 4.17 \text{ bar}$$

INTRODUCTION TO AEROSPACE PROPULSION



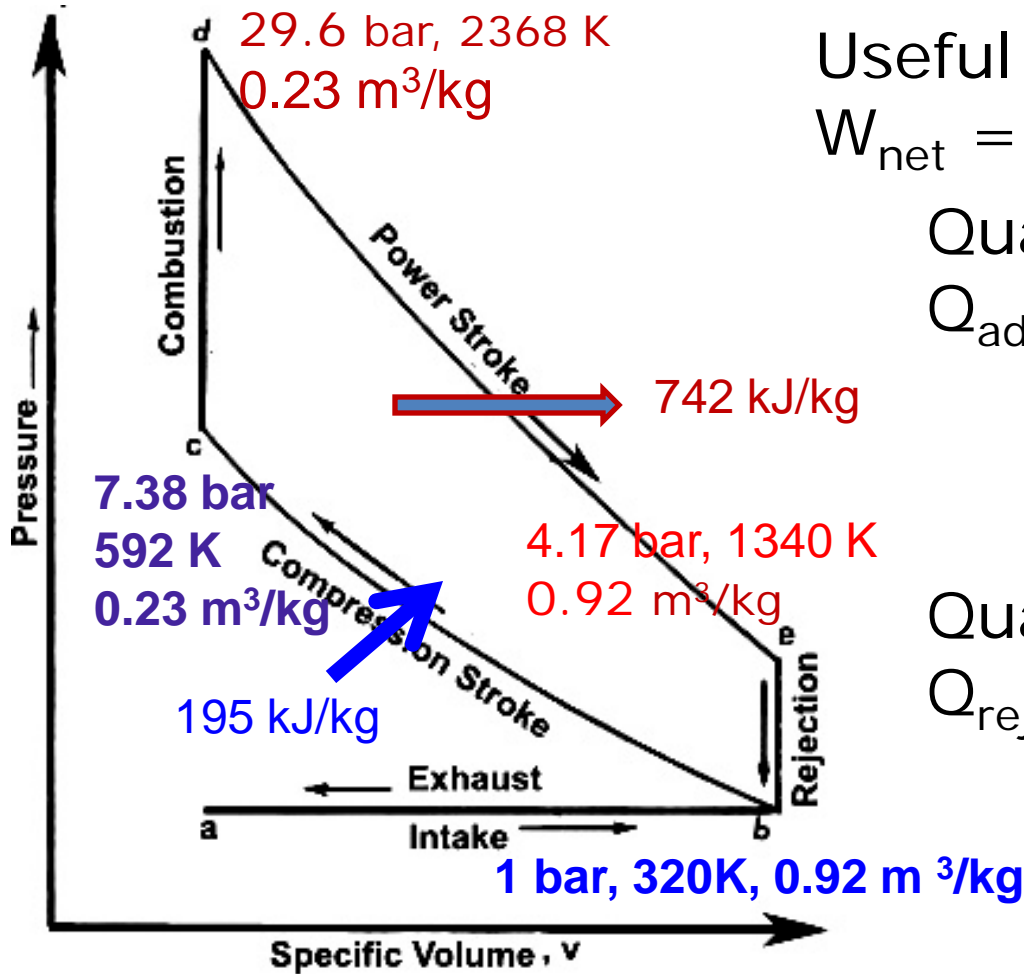
The power stroke work is given as :

$$\begin{aligned} \dot{W}_{\text{power}} &= \frac{1}{k-1} (p_d v_d - p_e v_e) \\ &= \frac{10^5}{0.4} (29.6 \times 0.23 - 4.17 \times 0.92) \\ &= 742.0 \text{ kJ/kg} \end{aligned}$$

The compression work is :

$$\begin{aligned} \dot{W}_{\text{compr}} &= \frac{1}{k-1} (p_b v_b - p_c v_c) \\ &= \frac{10^5}{0.4} (1 \times 0.92 - 7.38 \times 0.23) \\ &= -195 \text{ kJ/kg} \end{aligned}$$

INTRODUCTION TO AEROSPACE PROPULSION



Useful work is thus :

$$W_{\text{net}} = 743 - 195 = \mathbf{547 \text{ kJ/kg}}$$

Quantity of heat added is :

$$\begin{aligned} Q_{\text{add}} &= C_v(T_d - T_c) \\ &= 0.72(2368 - 592) \\ &= \mathbf{1280 \text{ kJ/kg}} \end{aligned}$$

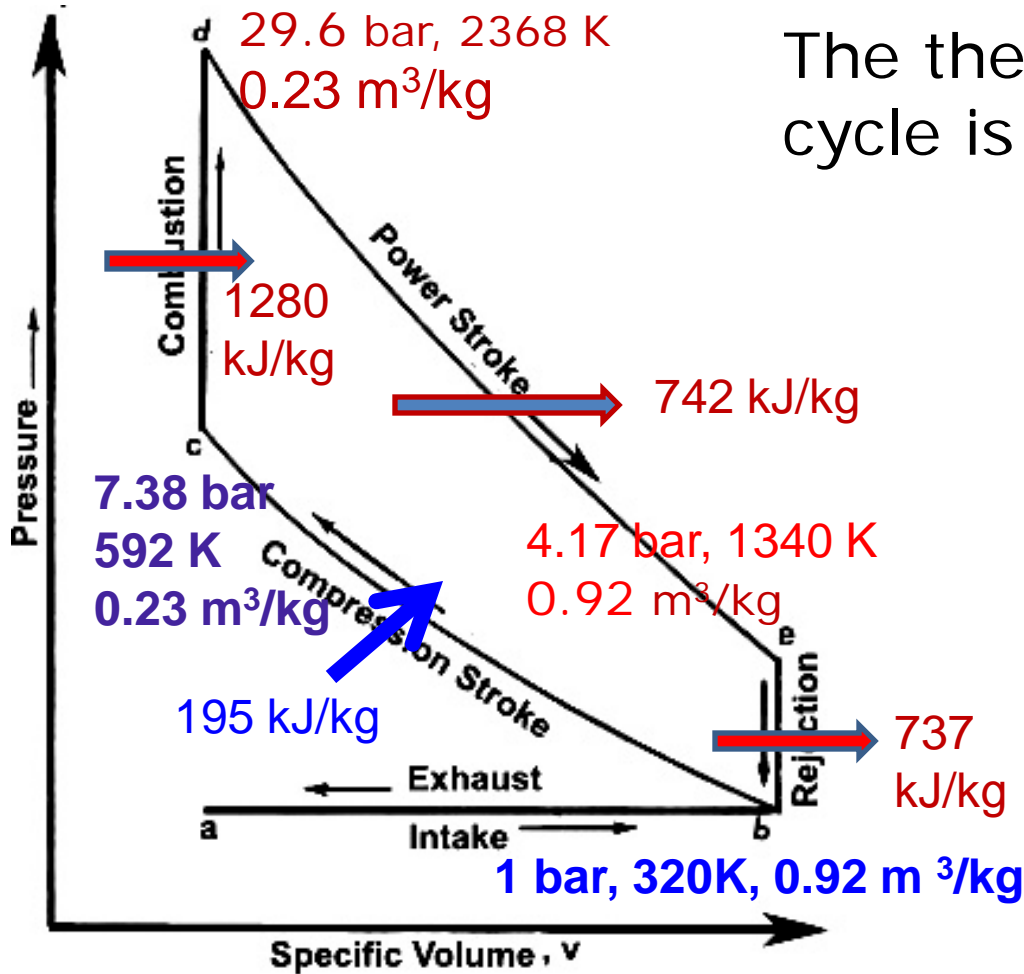
Quantity of heat rejected

$$\begin{aligned} Q_{\text{rej}} &= C_v(T_e - T_f) \\ &= 0.72(1340 - 320) \\ &= \mathbf{737 \text{ kJ/kg}} \end{aligned}$$

Heat utilised: 1280 - 737

$$Q_{\text{net}} = \mathbf{543 \text{ kJ/kg}}$$

INTRODUCTION TO AEROSPACE PROPULSION



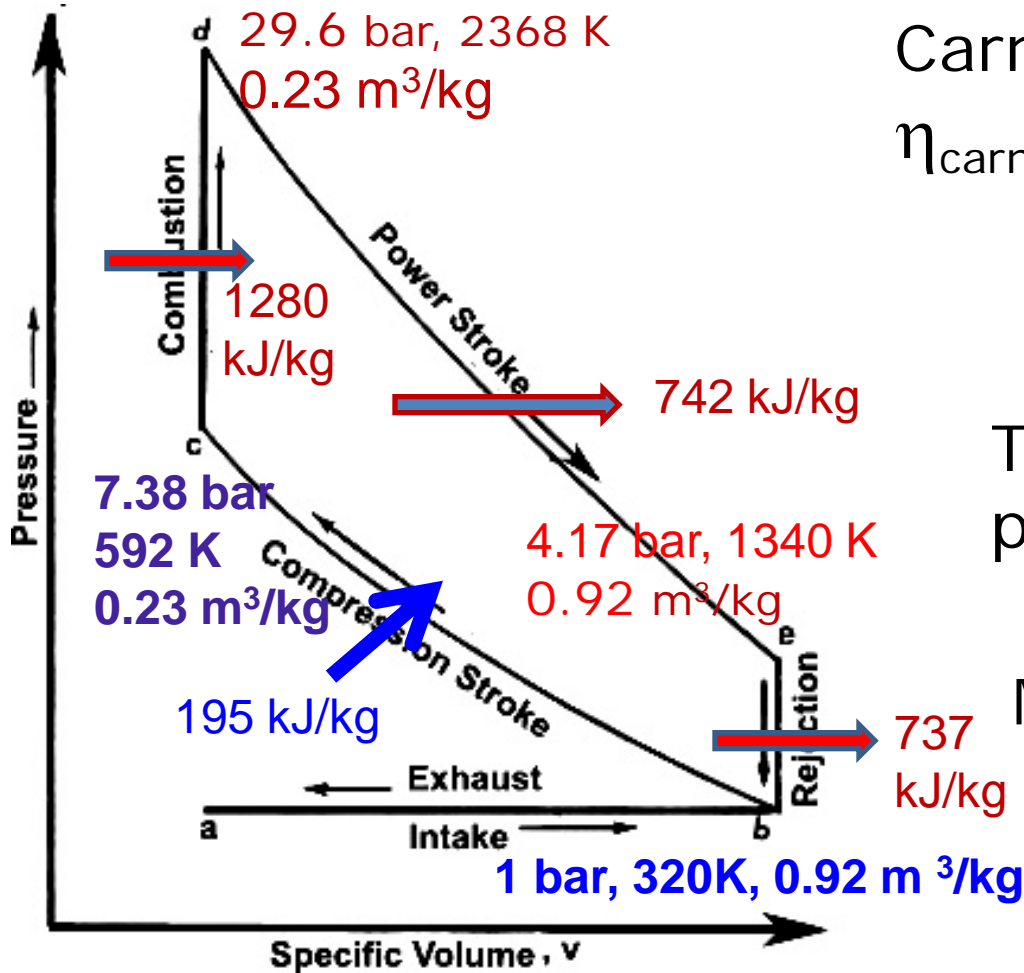
The thermal efficiency of the cycle is :

$$\begin{aligned} \eta_{th} &= Q_{net} / Q_{add} \\ &= 543 / 1280 \\ &= 0.425 \end{aligned}$$

Thermodynamically , thermal eff.

$$\begin{aligned} \eta_{th} &= 1 - \frac{1}{\omega^{k-1}} = 1 - \frac{1}{4^{0.4}} \\ &= 0.426 \end{aligned}$$

INTRODUCTION TO AEROSPACE PROPULSION



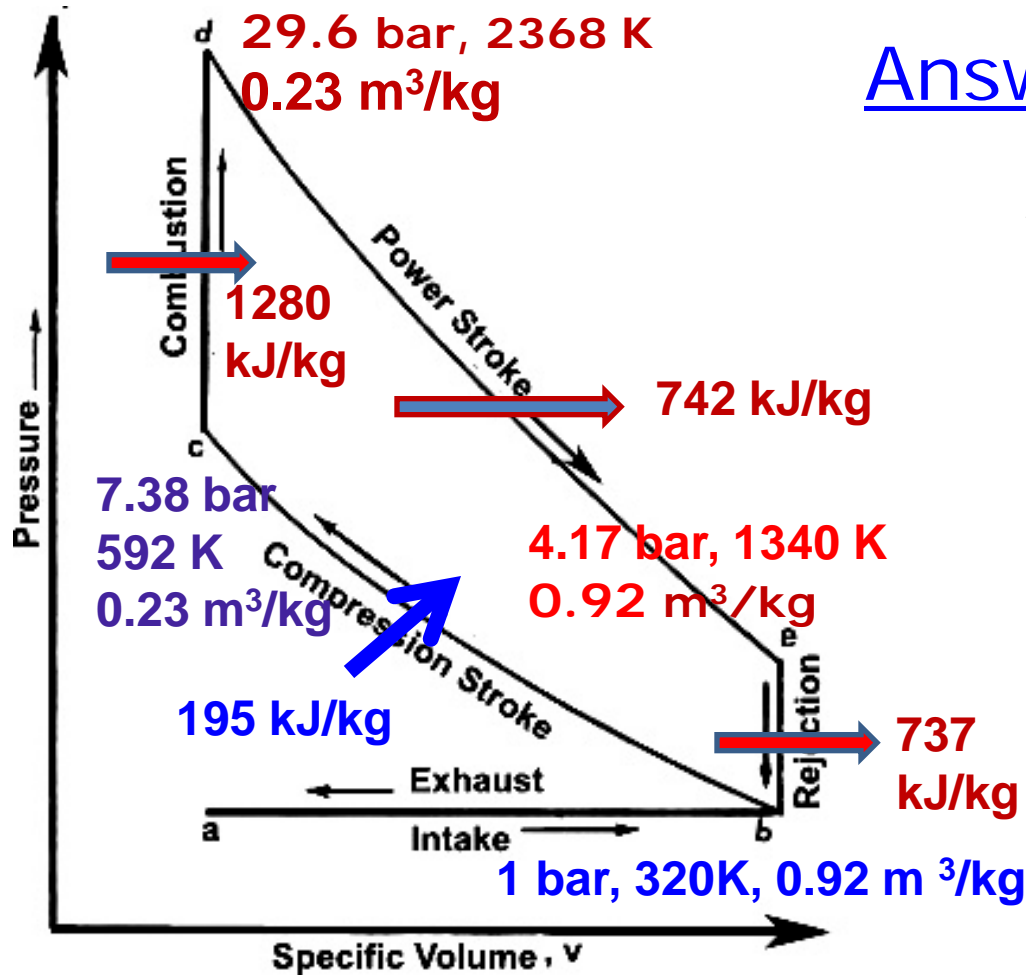
Carnot cycle efficiency is :

$$\begin{aligned} \eta_{\text{carnot}} &= 1 - T_b / T_d \\ &= 1 - 320 / 2368 \\ &= 0.865 \text{ or } 86.5\% \end{aligned}$$

The mean effective pressure is :

$$\begin{aligned} \text{MEP} &= W_{\text{net}} / (v_b - v_c) \\ &= 547,000 / 69000 \\ &= 7.9 \text{ bar} \end{aligned}$$

INTRODUCTION TO AEROSPACE PROPULSION



Answers

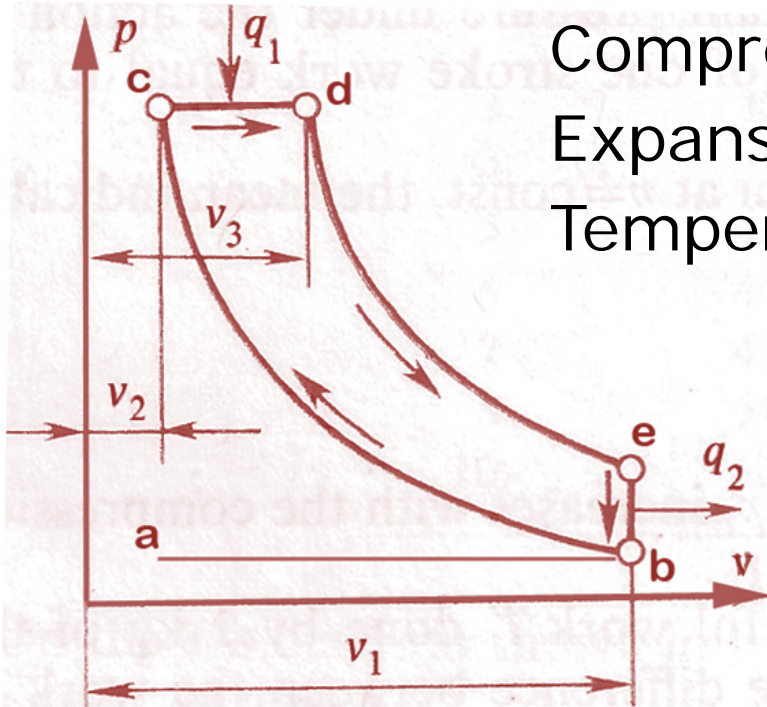
$$\eta_{\text{carnot}} = 86.5\%$$

$$\text{MEP} = 7.9 \text{ bar}$$

$$\eta_{\text{th}} = 0.425$$

- 2) For an ideal IC engine operating with combustion at **constant pressure**, given that it is operating with $p_a = 1$ bar, $T_a = 350$ K, compression ratio = 20, isobaric expansion ratio = 2.0. The working medium is air ($k = 1.4$ and $R = 287$ kJ/kg). For 1 kg of air calculate :
- (i) **Pressure and temperature at all cycle points**
 - (ii) Work done under various cycle legs
 - (iii) **Heat added or rejected during various cycle legs**
 - (iv) Carnot cycle efficiency
 - (v) **Indicated mean effective pressure**

INTRODUCTION TO AEROSPACE PROPULSION



Compression ratio : $\epsilon = v_b / v_c = 20$
 Expansion Ratio (c-d): $\delta = v_d / v_c = 2$
 Temperature Ratio: $\tau = T_d / T_b = ?$

$$v_b = R \cdot T_b / P_b = 287 \times 350 / 10^5 = \mathbf{1.0 \text{ m}^3/\text{kg}}$$

$$v_c = v_b / \epsilon = 1.0 / 20.0 = \mathbf{0.05 \text{ m}^3/\text{kg}}$$

$$p_c = p_b \cdot \epsilon^k = 1 \times 20^{1.4} = \mathbf{66.2 \text{ bar}}$$

$$T_c = p_c \cdot v_c / R = 66.2 \times 10^5 \times 0.05 / 287 = \mathbf{1155 \text{ K}}$$



INTRODUCTION TO AEROSPACE PROPULSION

Parameters at point **d** shall be computed from :

$$p_d = p_c = 66.2 \text{ bar}; \quad \& \quad v_d = v_c \times \delta = 0.05 \times 2 = 0.1 \text{ m}^3/\text{kg}$$

$$\text{At } T_d = T_c \times \delta = 1155 \times 2 = 2310 \text{ K}$$

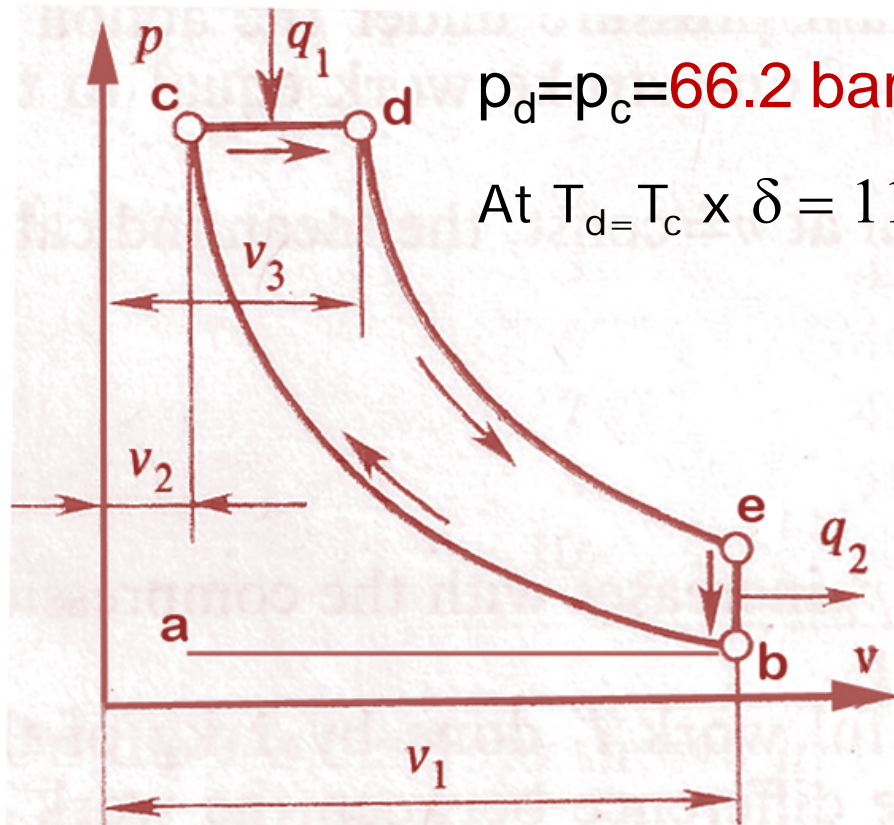
Now,

$$v_e = v_b = 1.0 \text{ m}^3/\text{kg}$$

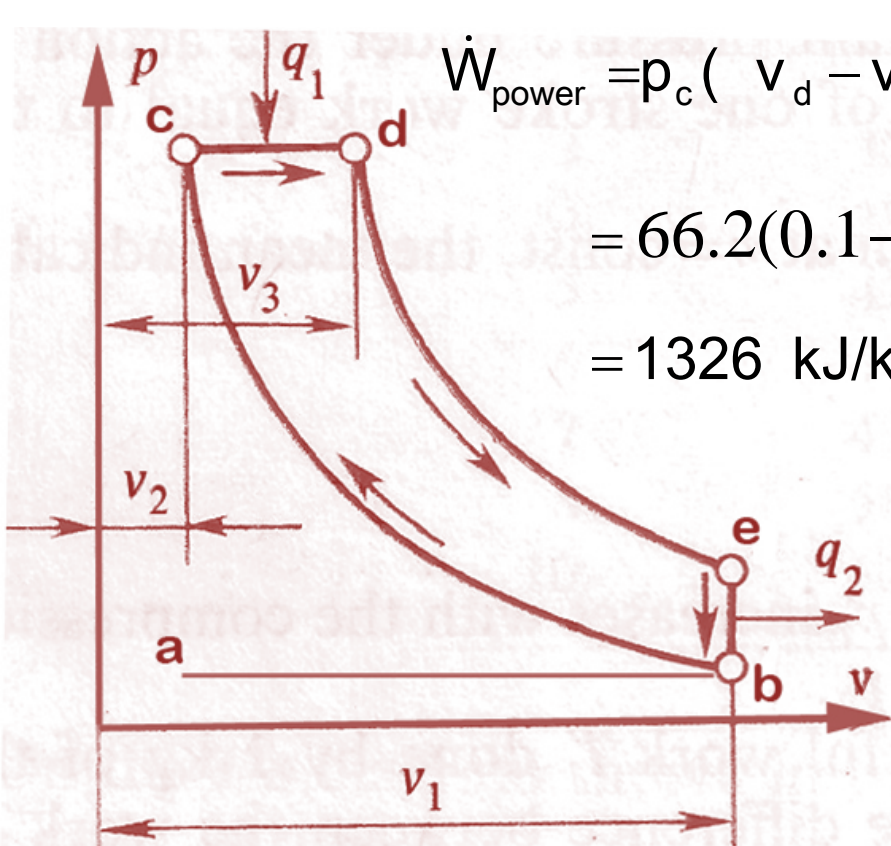
$$\text{using } \frac{T_e}{T_d} = \left(\frac{v_d}{v_e} \right)^{k-1}$$

$$T_e = 920 \text{ K}$$

$$\begin{aligned} P_e &= R \cdot T_e / v_e \\ &= 287 \times 927 / 1 \times 10^5 \\ &= 2.64 \text{ bar} \end{aligned}$$



INTRODUCTION TO AEROSPACE PROPULSION



$$\dot{W}_{\text{power}} = p_c (v_d - v_c) + \frac{1}{k-1} (p_d v_d - p_e v_e)$$

$$= 66.2(0.1 - 0.05) + \frac{10^5}{0.4} (66.2 \times 0.01 - 2.64 \times 1.0)$$

$$= 1326 \text{ kJ/kg}$$

Compression work

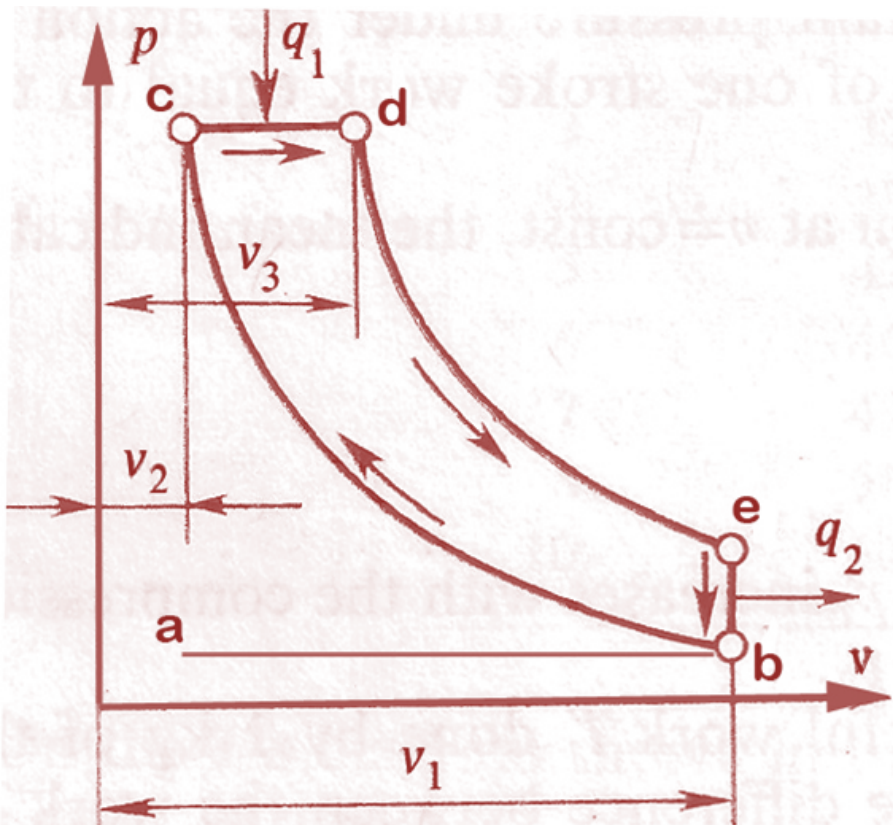
$$\dot{W}_{\text{compr}} = \frac{1}{k-1} (p_b v_b - p_c v_c)$$

$$= \frac{10^5}{0.4} (1 - 66.2 \times 0.05)$$

$$= -578 \text{ kJ/kg}$$

$$\text{Net work output} = 1326 - 578 = 748 \text{ kJ/kg}$$

INTRODUCTION TO AEROSPACE PROPULSION



Quantity of heat added is :

$$\begin{aligned}q_1 &= C_p(T_d - T_c) \\ &= 1.005(2310 - 1155) \\ &= \mathbf{1162 \text{ kJ/kg}}\end{aligned}$$

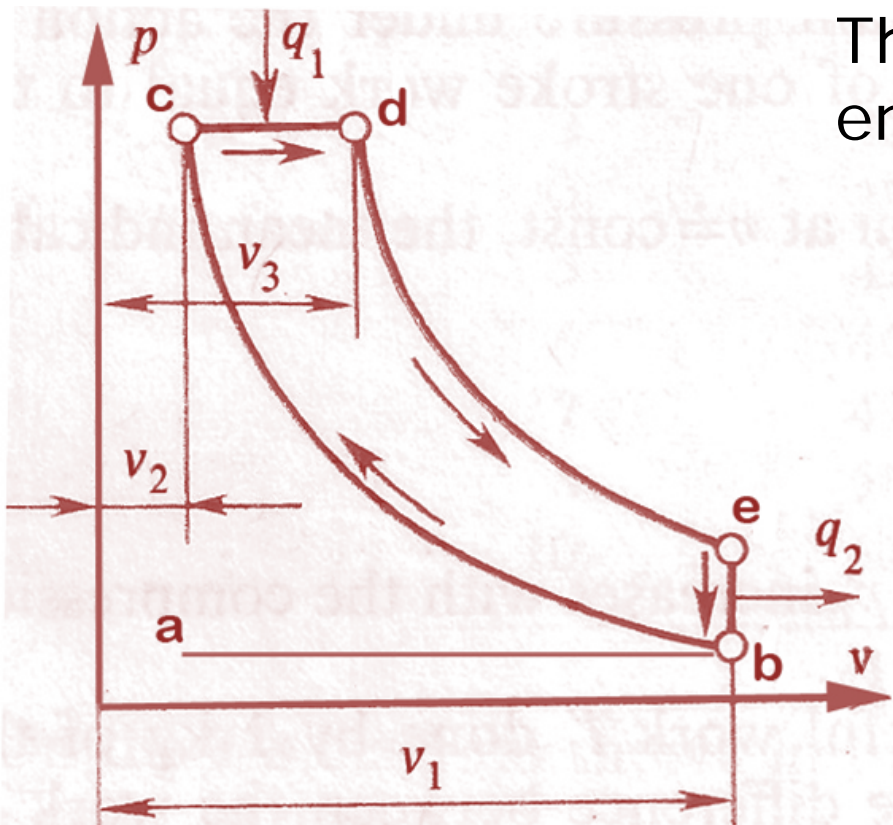
Quantity of heat rejected

$$\begin{aligned}q_2 &= C_v(T_e - T_b) \\ &= 0.72(920 - 350) \\ &= \mathbf{410 \text{ kJ/kg}}\end{aligned}$$

Heat utilised: 1162 – 410

$$Q_{\text{net}} = \mathbf{752 \text{ kJ/kg}}$$

INTRODUCTION TO AEROSPACE PROPULSION



The thermal efficiency of the engine is :

$$\begin{aligned}\eta_{th} &= Q_{net} / Q_{add} \\ &= 752 / 1162 \\ &= 0.648\end{aligned}$$

Cycle efficiency is:

$$\begin{aligned}\eta_{th} &= 1 - \frac{\delta^k - 1}{k \cdot \omega^{-1}} (\delta - 1) \\ &= 1 - \frac{2^{1.4} - 1}{1.4 \times 20^{0.4}} \\ &= 0.65\end{aligned}$$

This is derived for ideal diesel cycle

INTRODUCTION TO AEROSPACE PROPULSION

Answers

Indicated mean effective pressure

$$\text{IMEP} = W_{\text{net}} / (v_b - v_c)$$

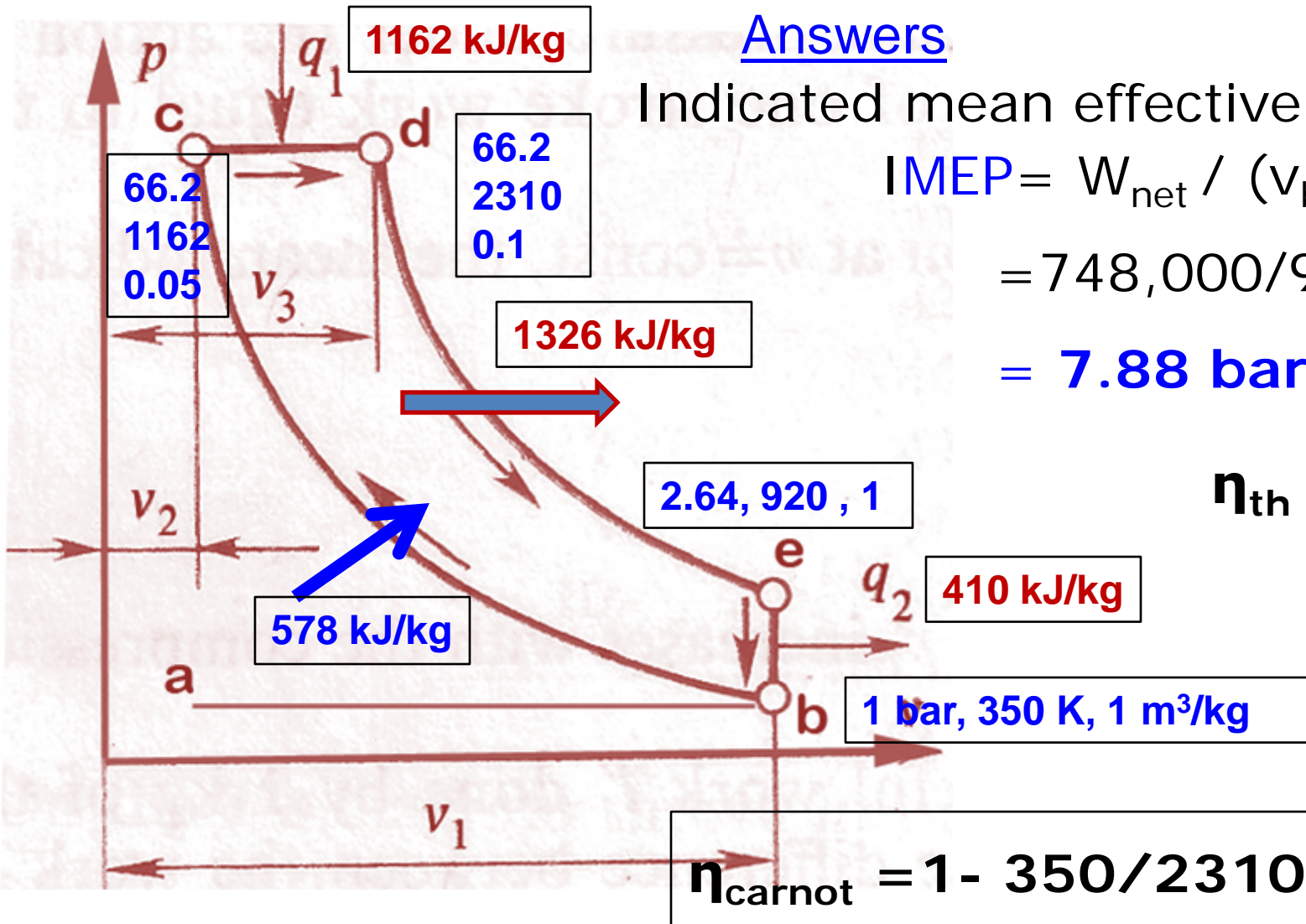
$$= 748,000 / 95,000$$

$$= 7.88 \text{ bar}$$

$$\eta_{\text{th}} = 0.648$$

$$2.64, 920, 1$$

$$\eta_{\text{carnot}} = 1 - 350 / 2310 = 0.85$$



Quiz questions - I

- 1) Which is more important : (i) Air charge per cycle , or (ii) Air charge per minute - for engine power performance estimation ?
- 2) Does Volumetric efficiency matter any more once supercharging is used in aircraft engines?
- 3) If High torque production coincides with high BMEP, what is the other operational requirements?
- 4) In IC engine parlance - what is the difference between (i) compression ratio, and (ii) pressure ratio?
- 5) Does a turbosupercharger provide higher efficiency of the engine, or that it only provides a continuous control mechanism for the supercharger ?

Quiz questions - II

- 6) Is very high supercharging beneficial at low altitude flying of aircraft ?
- 7) Is there is any limit to the degree of supercharging that can be applied to aircraft engines?
- 8) When does the intake and exhaust valve operation overlap? Does the design and timing of operation of these valve operations affect the engine performance ?
- 9) When should the engine produce (i) more Power (BHP), and (ii) more Torque – during an aircraft flight ?
- 10) For typical aircraft engines which fundamental parameter is kept high (design) for maximum power output?

Questions

- 1) A four-stroke engine produces an output of 420 kW when operating with mechanical efficiency of 87.5%. The fuel consumption is given as 164 kg/hr, when the air consumption is 2780 kg/hr, when the fuel heating value is prescribed as 44200 kJ/kg. Calculate :
- (i) IHP; (ii) FHP; (iii) air/fuel ratio;
 - (iv) Indicated thermal efficiency
 - (v) Brake thermal efficiency

[Ans : 600 HP; 75 HP; 15.2 ; 30% ; 26.2%]

Questions

2) An aircraft engine, equipped with a single stage supercharged engine, is flying at 7.0 km altitude (where ambient pressure is -41.1 kN/m^2 ; and the ambient temperature is $T = 241 \text{ K}$). The carburetor delivery condition is given as pressure = 75 mm H₂O, and the temperature = -24.4° C . Assuming ideal air ($k=1.4$) as working medium and no friction loss or heat loss in the supercharging, Calculate :

- (i) The Supercharging pressure ratio
- (ii) Corresponding Cylinder intake temperature

[Ans : 2.7 ; 73° C]

Questions

3) A four-stroke aircraft engine is running at 3600 rpm during the aircraft ground operation. The inlet air temperature is 15.6°C and the pressure is 1 bar. The engine has a total displaced volume of 4065.6 cc. The air/fuel ratio is 14:1. The bsfc is 0.377 kg/kW-hr for a power output of 83.5 kW.

Calculate the volumetric efficiency of the engine.

[Ans. 84.5%]

Next Class :

Propeller fundamentals