



# Jet Aircraft Propulsion

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Lecture 35

## Installed performance of Engines

- Engine design process ends with sizing of the engine to achieve the required thrust for a given airflow ( $\dot{m}_o$ ) through the engine, at the design point.
- When a powerplant is installed or attached to the body of the aircraft and flown with it the Installed thrust ( $T_F$ ) as experienced by the aircraft, comes out to be different from the design uninstalled thrust ( $F$ ) computed or bench tested for the isolated engine.
- The difference between  $T_F$  and  $F$  is often quite significant and may vary from one operating point to another of the engine or the aircraft.

- The *uninstalled thrust*,  $F$  represents only the result of the internal flow of air inside the engine.
- Installing the engine outside the fuselage induces aerodynamic forces ( $\mathbf{D}_{\text{engine}}$ ) that adds to the aircraft drag ( $D_{a/c}$ ).
- This is the “self-drag” of the engine (for external mounting of the engine).
- The installed thrust,  $T$ , must be the sum of uninstalled thrust,  $F$  and self-drag,  $\mathbf{D}_{\text{engine}}$ , which is determined along with the initial engine size, (i.e. uninstalled thrust estimation).
- Thus very presence of the engine, its inlet, nozzle and exhaust stream actually influence the flow over the entire aircraft it is affects the instantaneous thrust.

- From fundamental science, the engine performances favor higher bypass ratios, but the larger diameters and the resulting installation penalties prevent the final benefits.
- For high performance aircraft such as a fighter aircraft the engine is likely to be buried within the fuselage.
- The engine designer will be allowed to influence those parts that are believed to generate the bulk of the installation penalties, i.e. those affected by the inlet and exhaust flows.
- The inlet and nozzle external losses will be expressed as fraction of the uninstalled thrust,  $F$ .

Installed Thrust available for flying

$$T_F = F - \Phi_{inlet} F - \Phi_{nozzle} F$$

Flying thrust available is less than Engine Design Thrust

Or, 
$$F = T_F / (1 - \Phi_{inlet} - \Phi_{nozzle}) > T_F$$

Where,  $\Phi_s$  are the drag fractions of design thrust

$$\Phi_{inlet} = \frac{D_{inlet}}{F}$$

$$\Phi_{nozzle} = \frac{D_{nozzle}}{F}$$

$D_{inlet}$  : Drag due to engine inlet

$D_{nozzle}$  : Drag due to engine nozzle

- Note that  $\Phi_{\text{inlet}}$  &  $\Phi_{\text{nozzle}}$  will vary with flight condition and throttle setting for any engine, and vary from aircraft to aircraft slightly even for the same engine.
- Once the means of computing  $\phi_{\text{inlet}}$  &  $\phi_{\text{nozzle}}$  as a function of flight conditions (altitude, attitude and velocity) and throttle settings is found, the off-design computation method is used to “size” the engine.
- Starting from the “design point” engine and “mass flow”, the engine is “flown” (i.e. simulated) off-design at each critical flight condition at maximum power in accordance with the rated requirement.
- Next, either the engine mass flow (or the size) is adjusted until the **required** and the **available** thrust are equal at all flight conditions.

For each flight condition

$$\dot{m}_0 = \frac{F}{(F / \dot{m}_0)} = \frac{T_F}{(F / \dot{m}_0)(1 - \Phi_{inlet} - \Phi_{nozzle})}$$

For a climbing and accelerating (general) flight

$$\dot{m}_0 = \frac{W}{(F / \dot{m}_0)(1 - \Phi_{inlet} - \Phi_{nozzle})} \left[ \frac{(D_{a/c} + D_{eng})}{W} + \frac{1}{g} \frac{dV}{dt} + \frac{1}{V} \frac{dh}{dt} \right]$$

In order to find which of the flight conditions is most “demanding”, each  $\dot{m}_0$  is multiplied by the relevant  $(\dot{m}_{0design} / \dot{m}_{0-off-design})$  as obtained from engine off-design calculations. The largest product corresponds to the largest design of the engine, and hence the required engine size.

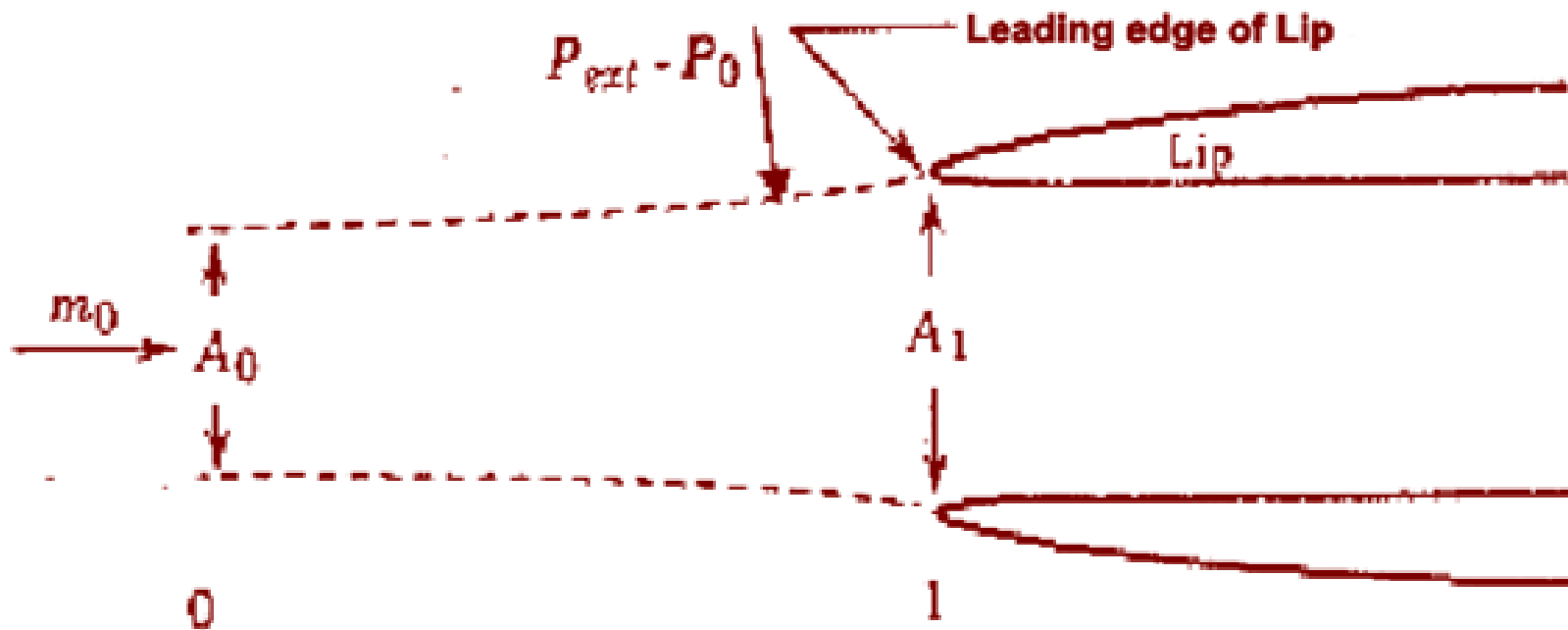


- This newly re-sized engine will be too large for all other flight conditions and performance at the other operating conditions must be obtained by throttling  $\dot{m}_0$ ,  $T_{04}$  (Turbine entry temperature) and  $T_{07}$  (nozzle temperature) until a new installed thrust is arrived at.
- This process needs to be completed before the installed behavior of the engine, i.e. its installed thrust and its installed fuel consumption rate is known with acceptable accuracy.

## Subsonic Inlet Drag

There is always a positive drag acting on the stream tube which encloses the air entering the engine intake

$$D_{add} = \int_0^1 (P_{ext} - P_0) dA$$



This is known as “additive drag” ( $D_{add}$ ) and is given as :

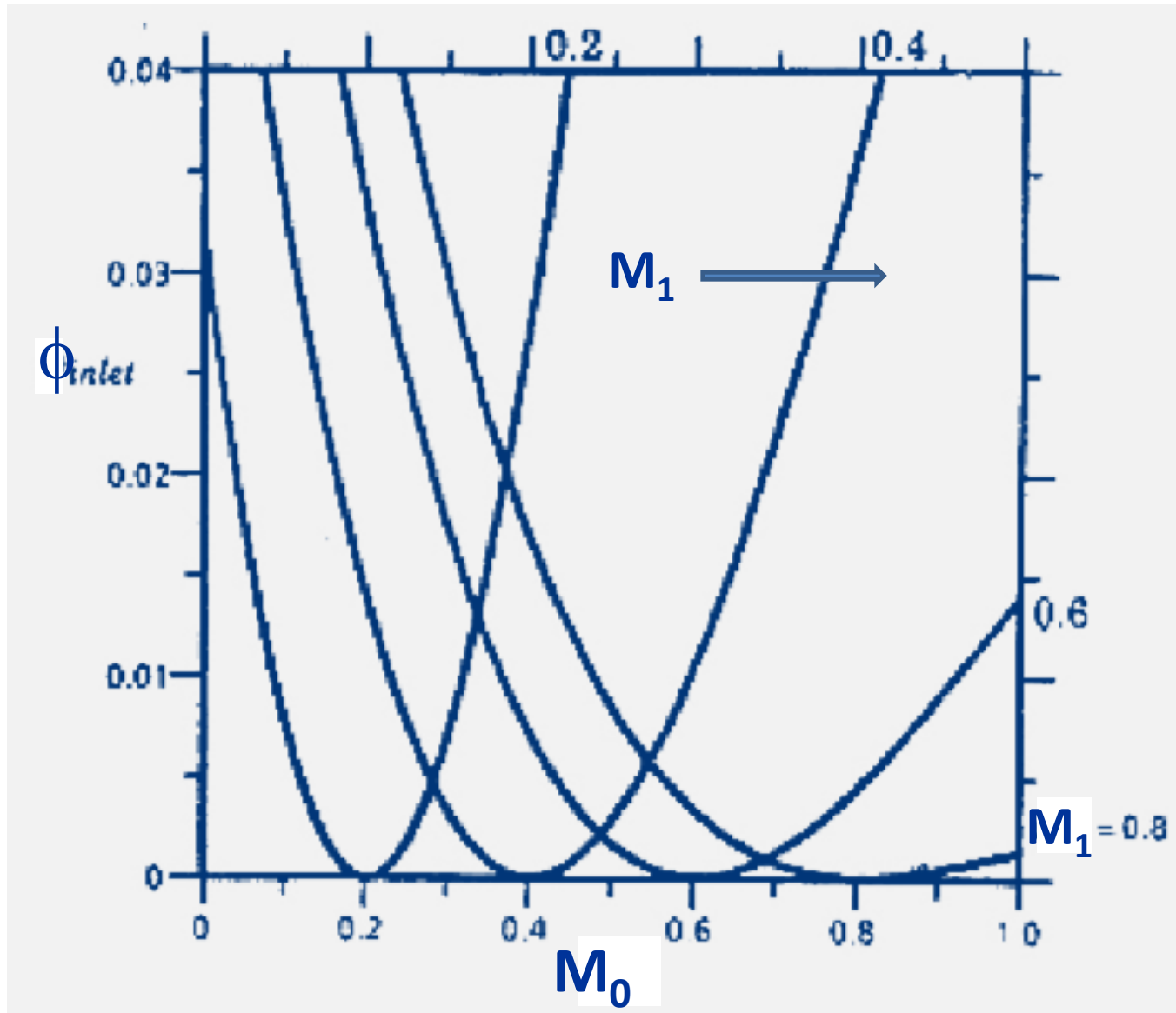
$$D_{add} = P_1 A_1 (1 + \gamma M_1^2) - P_0 A_0 \left( \frac{A_1}{A_0} + \gamma M_0^2 \right)$$

Inlet Drag fraction

$$\Phi_{inlet} = \frac{D_{add}}{F}$$

$$\Phi_{inlet} = \frac{D_{add}}{\dot{m}_0 (F / \dot{m}_0)} = \frac{\left( \frac{M_0}{M_1} \right) \left( \sqrt{\frac{T_1}{T_0}} \right) (1 + \gamma M_1^2) - P_0 A_0 \left( \frac{A_1}{A_0} + \gamma M_0^2 \right)}{\frac{F \gamma M_0}{\dot{m}_0 a_0}}$$

Which can be evaluated for any set of values of  $M_0$ ,  $M_1$ ,  $a_0$  and  $F/\dot{m}_0$

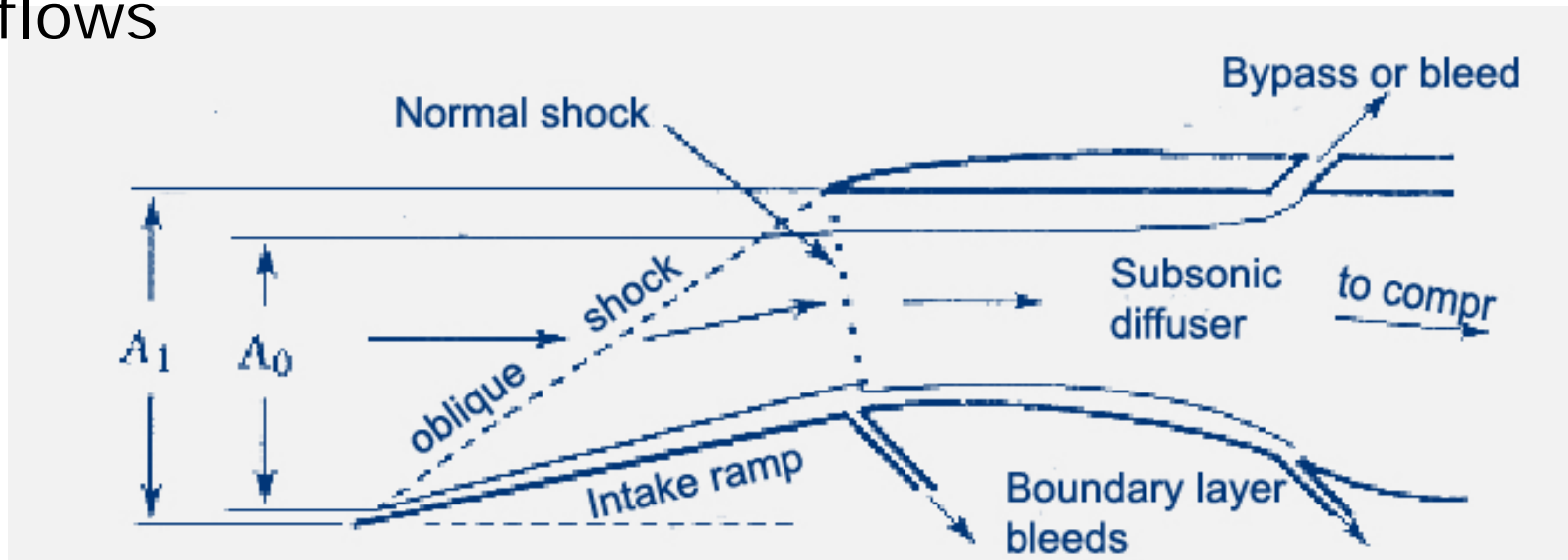


## Conclusions on Intake installation drag:

- $\Phi_{\text{inlet}}$  is not large if  $M_0$  is near  $M_1$  and the entering stream tube experiences no change in flow area.
- For the usual range of subsonic flight, it is desirable to keep  $M_1$  in the vicinity of 0.4-0.6
- High values of  $\Phi_{\text{inlet}}$  occur at  $M_0=0$ , at Take off, is in the range of 0.5-1.

## Supersonic Inlet Drag

The supersonic inlet drag is estimated to be equal to the momentum change of the bypass and bleed flows

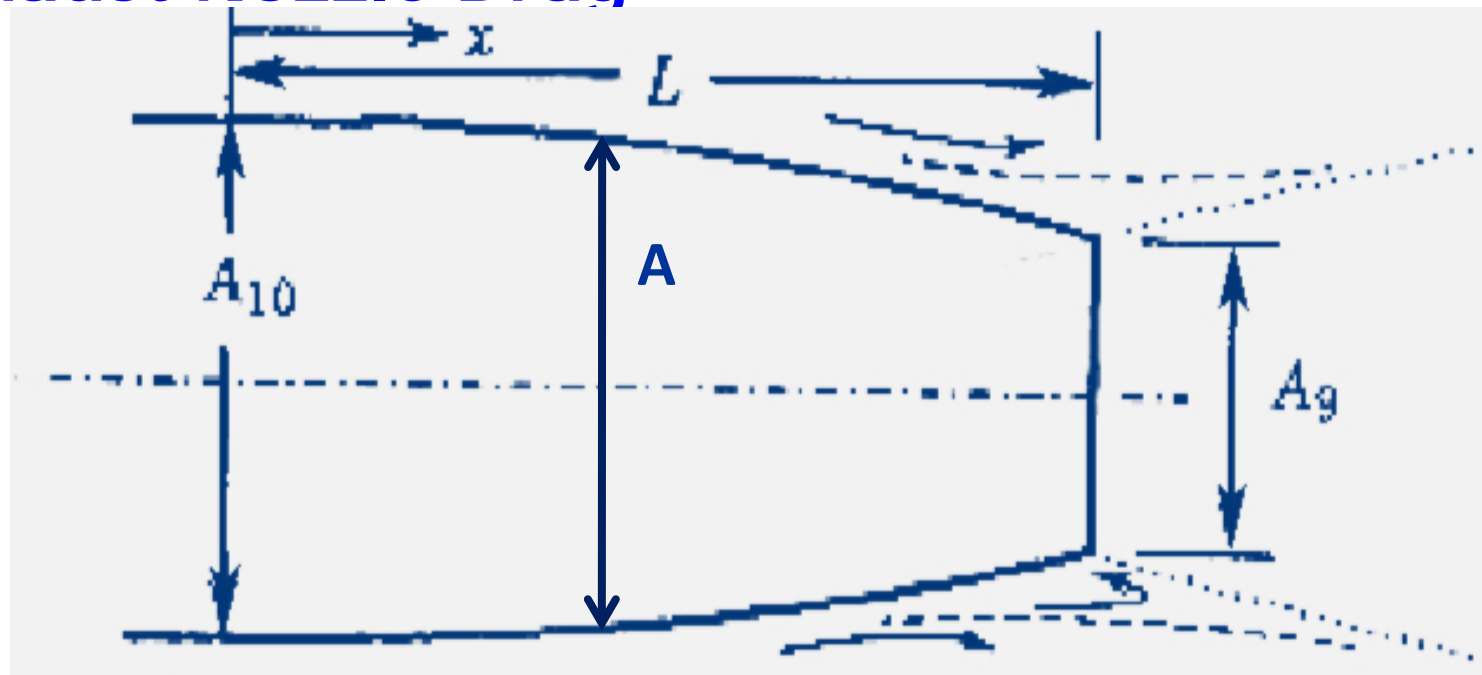


Supersonic Inlet Flow Model

$$\Phi_{inlet} = \frac{(A_1 / A_0 - 1) \left( M_0 - \sqrt{\frac{2}{\gamma + 1} + \frac{(\gamma - 1)M_0^2}{\gamma + 1}} \right)}{(Fg / \dot{m}_0 a_0)}$$

Once  $A_1$  has been selected, this equation can be directly evaluated at any given flight condition ( $P_0$ ,  $T_0$  and  $M_0$ ) and engine power setting (i.e.  $A_0$  and  $F.g/m_0$ ). Note that  $\phi_{inlet}$  approaches zero when (i)  $M_0$  approaches unity and (ii) when  $A_0$  approaches  $A_1$  (sized), so that  $\phi_{inlet}$  can be useful when it is evaluated far from both the conditions.

## Exhaust Nozzle Drag



For predicting the exhaust nozzle pressure drag in subsonic and supersonic conditions correlation method has been developed based on "*integral mean slope*"

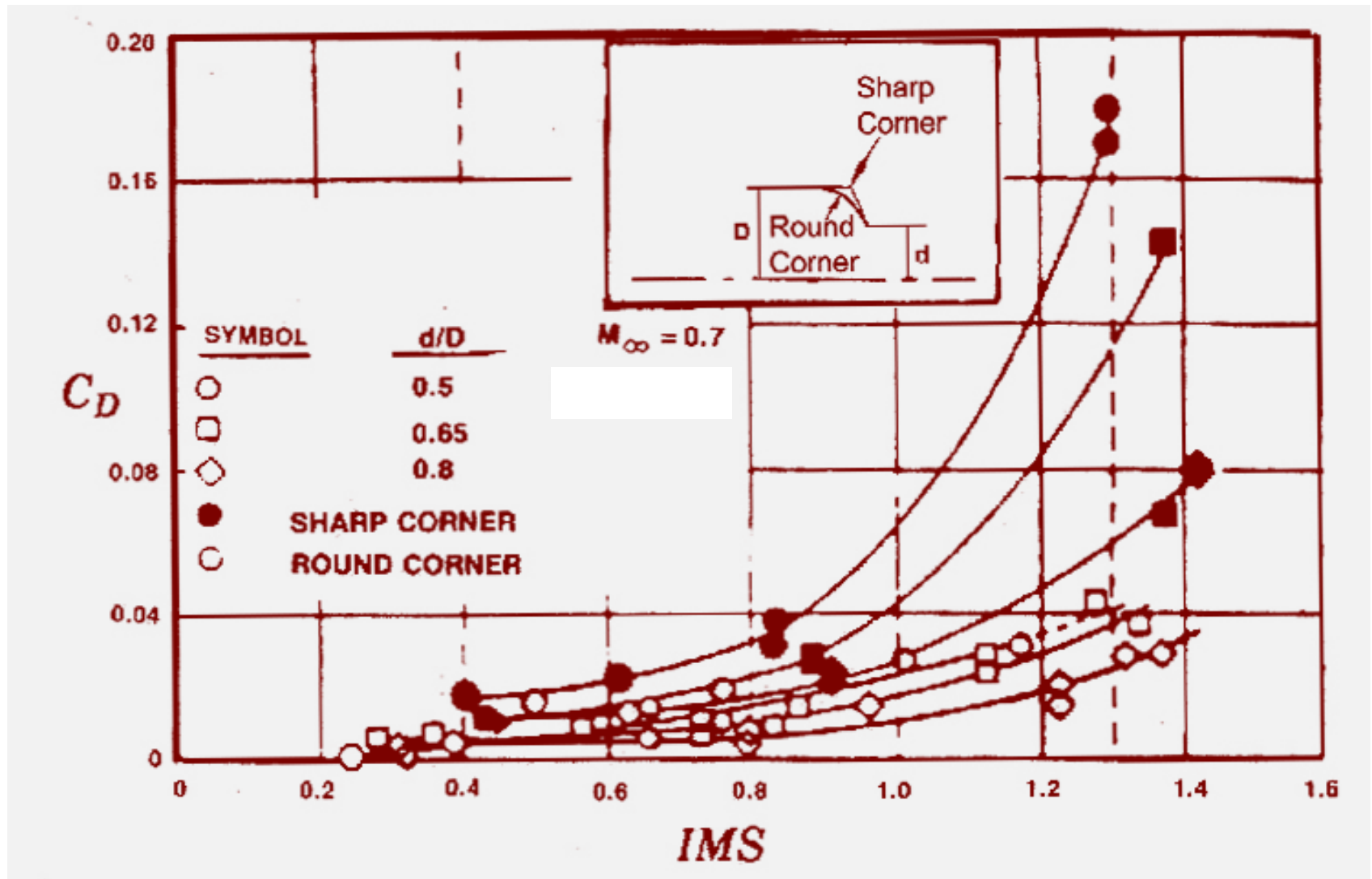


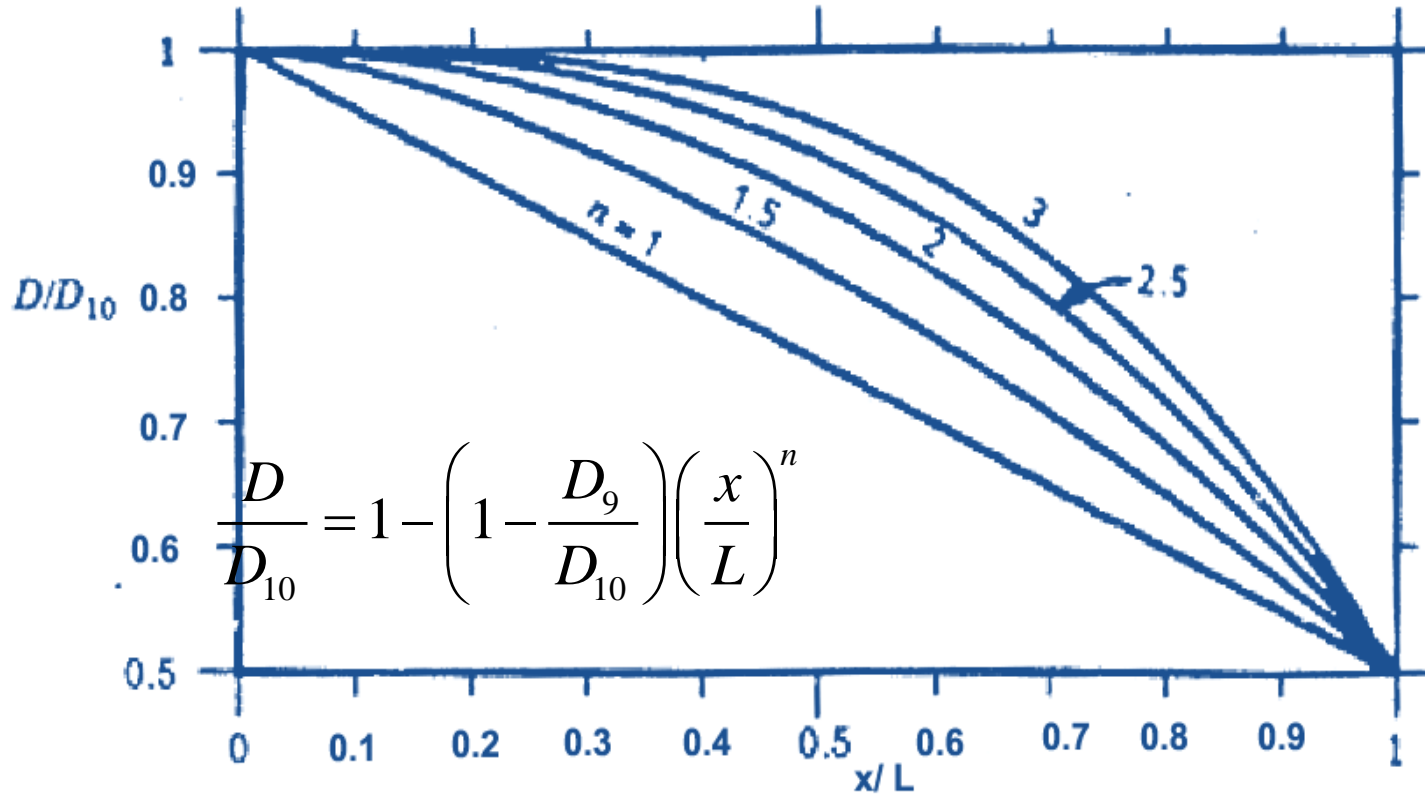
**"integral mean slope"** is defined by the equation  
*(Integral mean slope captures the slope of the nozzle external surface contour)*

$$IMS = \frac{1}{\left(1 - \frac{A_9}{A_{10}}\right)} \int_1^{\frac{A_9}{A_{10}}} \frac{d\left(\frac{A}{A_{10}}\right)}{d\left(\frac{x}{R_{10} - R_9}\right)} d\left(\frac{A}{A_{10}}\right)$$

For Quick Practical solution

$$IMS \cong 1.8 \left(\frac{D_{10} - D_9}{L}\right) \left(1 - \frac{D_9}{D_{10}}\right)$$





Nozzle installation penalty  
can be computed from

$$\Phi_{nozzle} = \frac{D_{nozzle}}{F} = \frac{q_0 C_D (A_{10} - A_9)}{\dot{m}_0 (F / \dot{m}_0)}$$

Next Class :

Problem solving for Engine matching  
and Tutorials