

Chapter 5

1. In gas separation by membrane, why gas film resistance is negligible?

Ans: High diffusivity of gaseous components.

2. In gas separation which resistance is dominating?

Ans: membrane resistance.

3. For complete mixing model in case of gas separation, find maximum composition of

reject stream if, $\alpha^* = 10$; $\frac{P_l}{P_h} = \frac{1}{60}$; $x_f = 0.3$;

$$x_{om} = \frac{x_f \left[1 + (\alpha^* - 1) \left(\frac{p_l}{p_n} \right) (1 - x_f) \right]}{\alpha^* (1 - x_f) + x_f}$$

Ans:

$$\alpha^* = 10; \quad \frac{p_l}{p_h} = \frac{1}{60}; \quad x_f = 0.3$$

$$x_{om} = -\frac{\alpha^*(1-x_f) + x_f}{\alpha^*(1-x_f) - 1 + (\alpha^* - 1)\left(\frac{p_l}{p_h}\right)(1-x_f)}$$

$$x_{om} = \frac{0.3 \left[1 + 9 \times \frac{1}{60} \times 0.7 \right]}{10 \times 0.7 + 0.3}$$

$$= \frac{0.3 \left[1 + 9 \times \frac{1}{60} \times 0.7 \right]}{10 \times 0.7 + 0.3}$$

=0.045

4. Counter current model in gas separation is like

Ans: (b)

5. Find membrane area to separate air using a membrane 0.002 cm thick with oxygen

permeability $P_A = 400 \times 10^{-10} \frac{cm^3(STP)cm}{s.cm^2.cmHg}$ and $\alpha^* = 8$ for permeability ratio of oxygen

and nitrogen. Feed rate, $q_f = 10^6 \text{ cm}^3/\text{s}$ and $\theta = 0.3$; $P_h = 150 \text{ cm Hg}$ and $P_l = 10 \text{ cm Hg}$.

Assume complete mixing model, calculate permeate composition, reject composition and membrane area.

Ans:

$$t = 0.002 \text{ cm}; \quad \alpha^* = 8; \quad P_A = 400 \times 10^{-10}; \quad q_f = 10^6 \text{ cm}^3/\text{s}; \quad \theta = 0.3$$

$$p_h = 150 \text{ cm Hg}; \quad p_l = 10 \text{ cm Hg}; \quad x_f = 0.21$$

$$\begin{aligned} a_1 &= \theta + \frac{p_l}{p_h}(1-\theta) - \alpha^* \theta - \alpha^* \frac{p_l}{p_h}(1-\theta) \\ &= 0.3 + \frac{1}{15} \times 0.3 - 8 \times 0.3 - 8 \times \frac{1}{15} \times 0.7 \\ &= -2.45 \end{aligned}$$

$$\begin{aligned} b_1 &= 1 - \theta - x_f - \frac{p_l}{p_h}(1-\theta) + \alpha^* \theta + \alpha^* \frac{p_l}{p_h}(1-\theta) + \alpha^* x_f \\ &= 1 - 0.3 - 0.21 - \frac{1}{15} \times 0.7 + 8 \times 0.3 + 8 \times \frac{1}{15} \times 0.7 + 8 \times 0.21 \\ &= 4.897 \end{aligned}$$

$$c_1 = -\alpha^* x_f = -8 \times 0.21 = -1.68$$

$$y_p = \frac{-b_1 + \sqrt{b_1^2 - 4a_1c_1}}{2a_1}$$

$$= \frac{-4.897 + \sqrt{4.897^2 - 4 \times (-2.45) \times (-1.68)}}{2 \times (-2.45)}$$

$$= 0.44$$

$$x_0 = \frac{x_f - \theta y_f}{1 - \theta}$$

$$= \frac{0.21 - 0.3 \times 0.44}{1 - 0.3}$$

$$= 0.11$$

$$A_m = \frac{\theta q_f y_p}{\left(-\frac{p_A}{t} \right) (p_h x_0 - p_l y_p)}$$

$$= \frac{0.3 \times 10^6 \times 0.44}{\left(-\frac{400 \times 10^{-10}}{0.002} \right) (150 \times 0.11 - 10 \times 0.44)}$$

$$= \frac{132000}{2 \times 10^5 \times 12.1}$$

$$= 5.45 \times 10^8 \text{ cm}^2$$