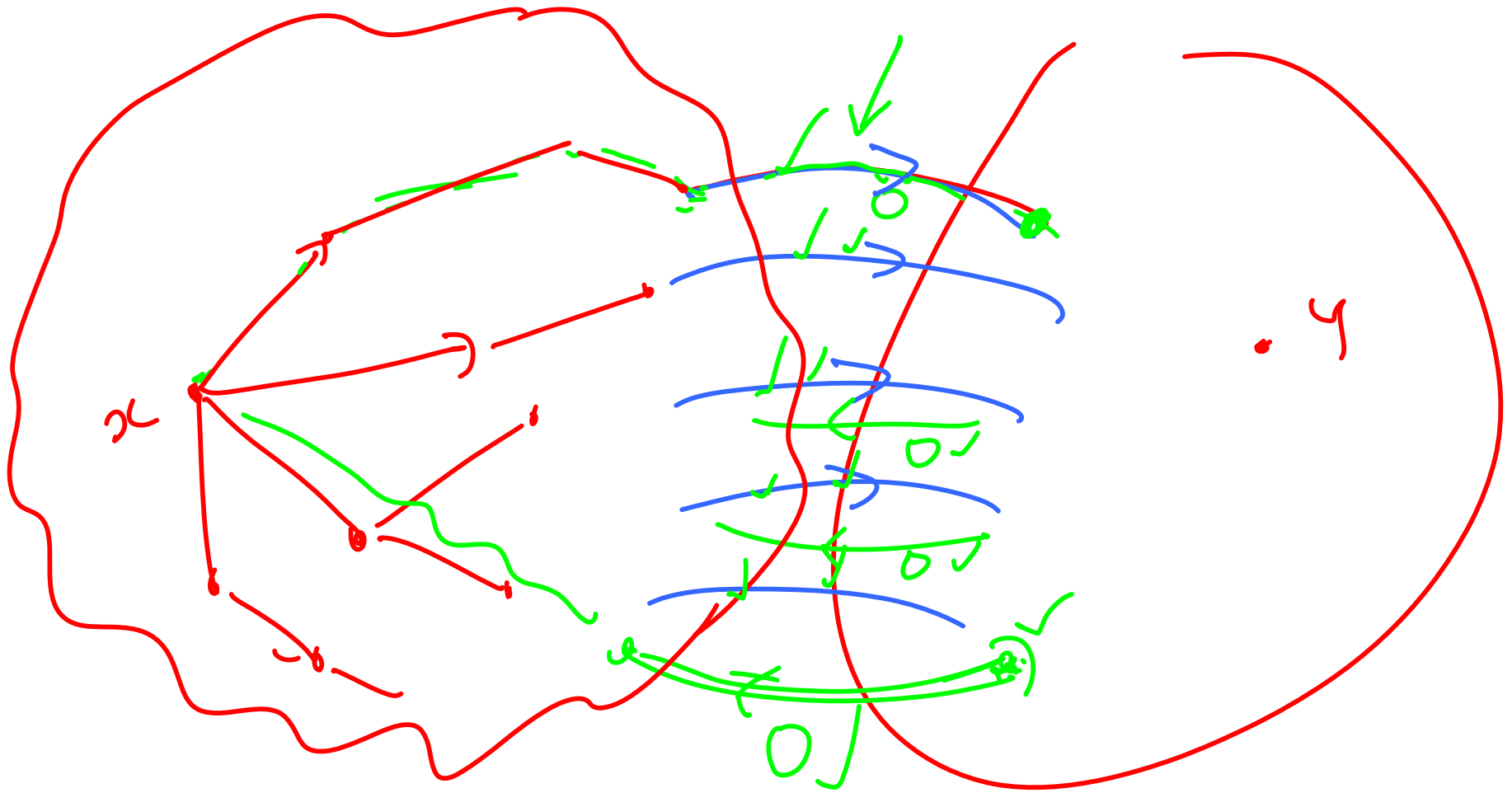


$$f' \leftarrow f$$



①  $X = \{x\}$ ,  $p(v) = \emptyset \quad \forall v \in V$

② While (there is either an  $f$ -unsaturated arc ~~or~~  $a = (u, v)$  or an  $f$ -positive arc  $a = (v, u)$  ~~with~~ with  $u \in X$  and  $v \in V - X$ , do

$$X = X \cup \{v\},$$

$$p(v) = u$$

end (while)

If  $y \in X$ , then find  $\varepsilon(P)$   
 $= \min \{ \varepsilon(a) : a \in P \}$

where  $P$  is the  $x$ - $y$  path defined by  
the pred. fn.  $p$ .

for a forward arc  $a$  of  $P$

$$f(a) = \underline{f(a) + \varepsilon(P)}.$$

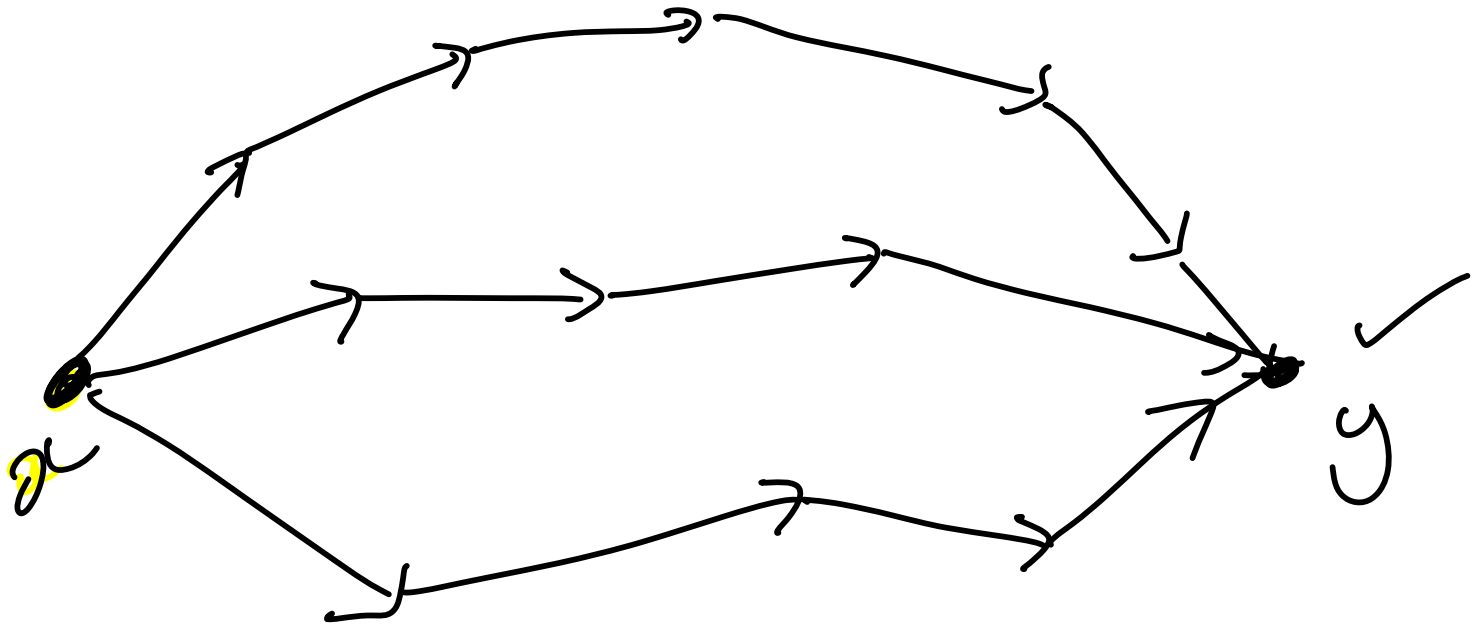
for a reverse arc  $a$  of  $P$

$$f(a) = \underline{\underline{f(a) - \varepsilon(P)}}$$



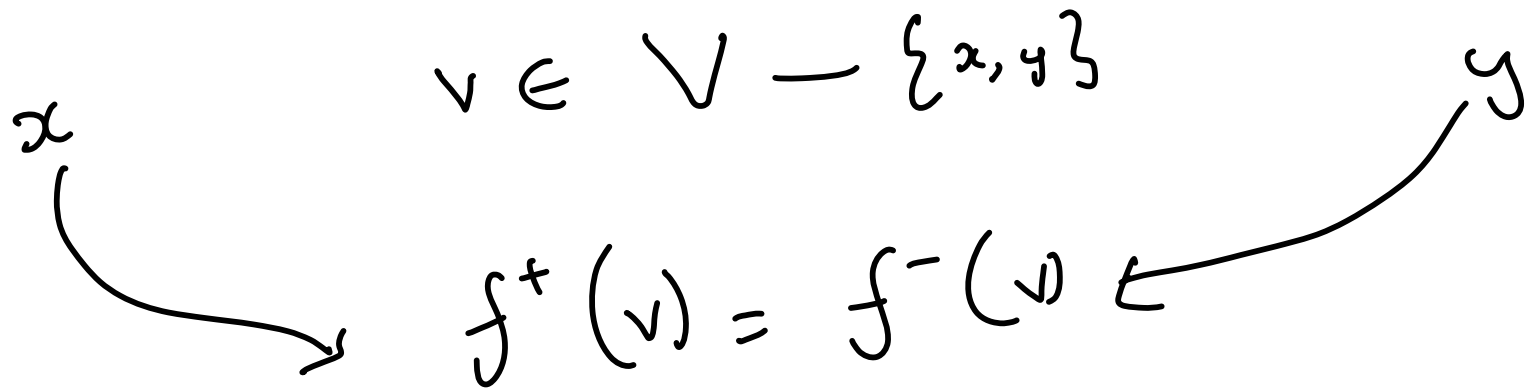
return  $(f, \partial^{\dagger}(x))$



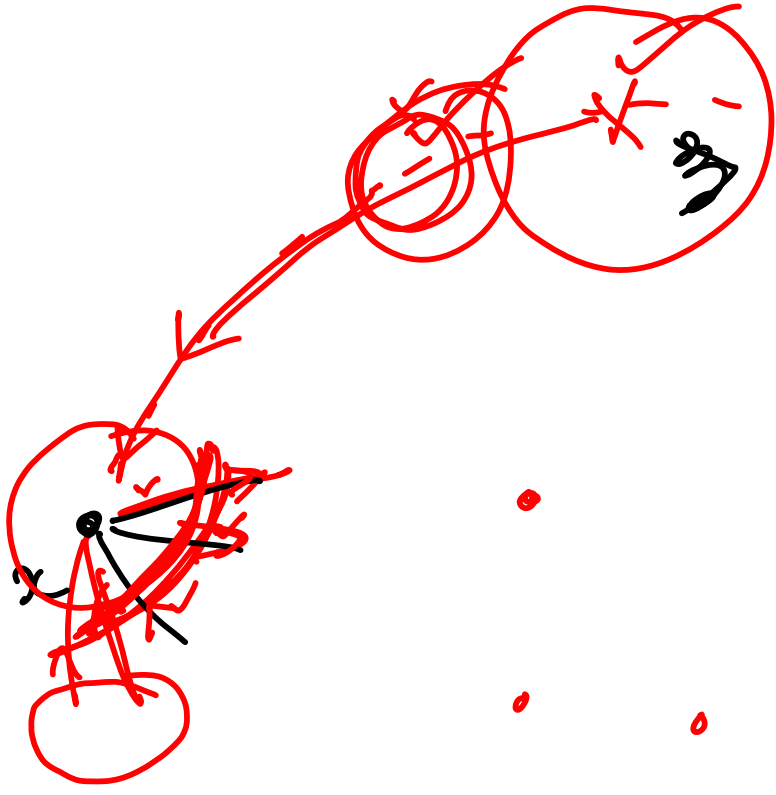




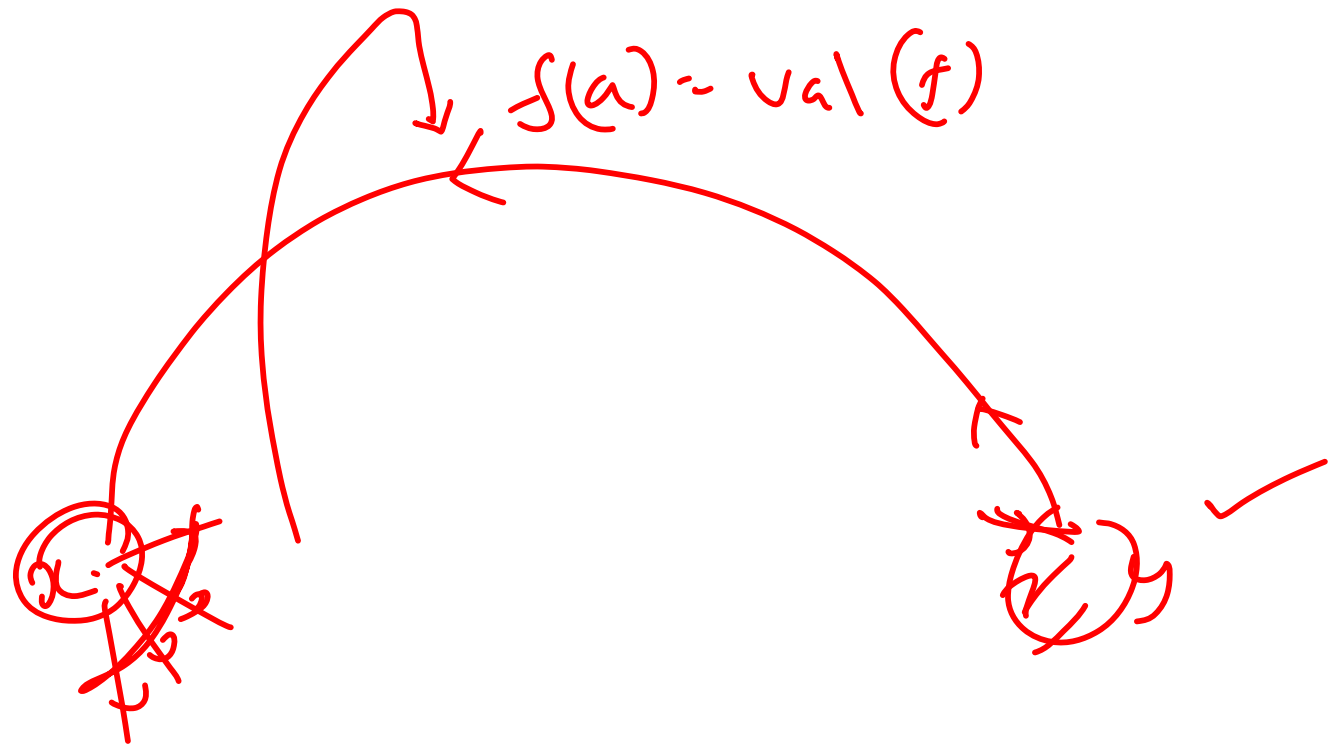
# Circulations ✓

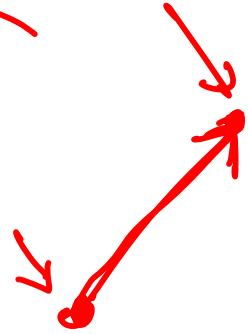
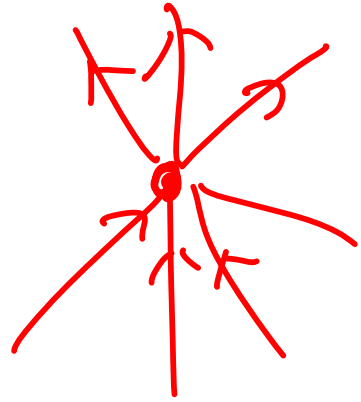


If for all  $v \in V$ ,  $f^+(v) = f^-(v)$



.





$M$

$(i, i)$

$$= \begin{matrix} & a_1 & a_2 & \dots & a_n \\ \begin{matrix} 1 \\ 2 \\ 3 \\ \vdots \\ s \end{matrix} & \begin{bmatrix} 0 & 0 & \dots & 1 & \dots \\ 0 & 0 & \dots & 0 & \dots \\ 0 & 0 & \dots & 0 & \dots \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & \dots & 0 & \dots \end{bmatrix} \end{matrix}$$

$\bullet \quad \mathcal{M} f = \begin{bmatrix} a_1 & 0 & \dots & 0 \\ a_2 & 0 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ a_m & 0 & \dots & 0 \end{bmatrix} \begin{bmatrix} f(a_1) \\ f(a_2) \\ \vdots \\ f(a_m) \end{bmatrix}$

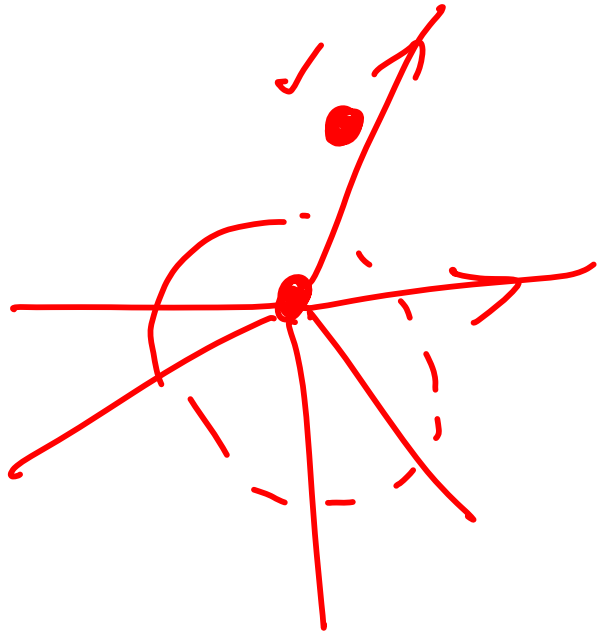
$$\begin{array}{l}
 a_1 \rightarrow \begin{bmatrix} f(a_1) \\ \vdots \\ \textcircled{1} \\ \vdots \end{bmatrix} \\
 a_2 \rightarrow \begin{bmatrix} f(a_2) \\ \vdots \\ \vdots \\ \vdots \end{bmatrix} \\
 \vdots \\
 a_i \rightarrow \begin{bmatrix} f(a_i) \\ \vdots \\ \vdots \\ \vdots \end{bmatrix} \\
 \vdots \\
 a_m \rightarrow \begin{bmatrix} f(a_m) \\ \vdots \\ \vdots \\ \vdots \end{bmatrix}
 \end{array}$$

$$\begin{array}{l}
 \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_m \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix} \\
 \begin{bmatrix} 1 \\ 2 \\ 3 \\ \vdots \\ m \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}
 \end{array}$$

"f"

← support

$$\{a \in A : f(a) \neq 0\}$$



$$f_c(a) = 1$$

$$f_c(a) = -1$$

