Assignment # 1

Review of Solid Mechanics

- 1. In a two dimensional problem without resorting to the Mohr's circle approach, how would you find the principal stresses and their corresponding directions uniquely?
- 2. The stress tensor with respect to x, y, z axes is given as $[\tau]$. If the x and y axes are given a rotation θ_z , determine the stress tensor in the new transformed co-ordinate system x', y' and z'.
- 3. What is the mathematical definition of a free surface? Specify the stress tensor on free outward corners. Justify your answer.
- 4. Draw the BMD and SFD of a three point bend specimen. Sketch the variation of normal stress and shear stress distribution across a general cross-section as specified by the engineering theory of beams. Mention the procedure for solving the problem using theory of elasticity. Compare the two solutions for shear stress distribution along a line very close to the central load.
- 5. (a). Derive the compatibility conditions in terms of stress components for plane stress and plane strain problem. Comment on the influence of elastic constants.
 - (b). Write down the Beltrami-Mitchell equations of equilibrium. Comment on the influence of elastic constants.

